

## Course Notes / Note de curs



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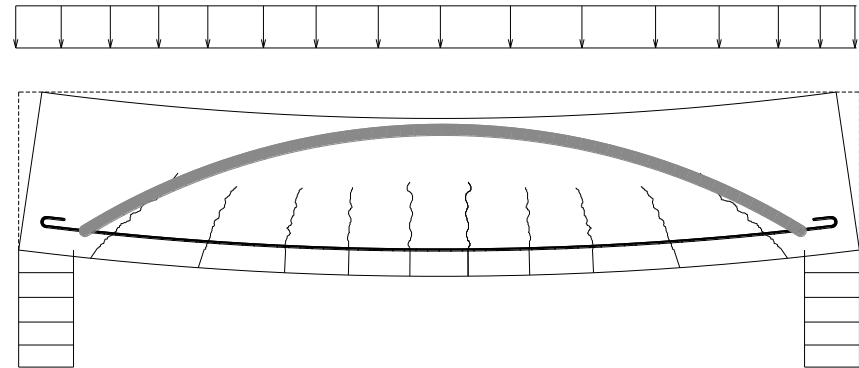
# 4.1 REINFORCEMENT ANCHORAGE

## 4.2 WORKING STAGES OF RC ELEMENTS

## 4.3 DURABILITY OF RC

## Reinforcement anchorage in concrete

The concrete does not withstand tension, therefore associated with steel reinforcements. After concrete cracking, reinforcement is overtake tensile stresses of the elements.



⇒ Must be **ensure cooperation** between concrete and reinforcement, i.e. reinforcement slipping in concrete, by a suitable **anchorage**.

## Anchorage / Ancorarea

**Reinforcement anchorage in concrete is achieved through:**

- Bond
- Hooks or Heads of the bars
- Special anchorage

## Concrete and reinforcement works together due to bond.

Bond → defined by the bond strength,  $f_b$

→ is produced by

- a) adhesion between concrete and steel
- b) friction between reinforcement & concrete
- c) clenching of concrete between bar ribs

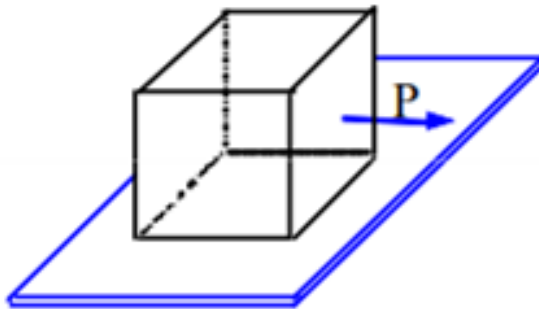
## Anchorage / Ancorarea

**Concrete and reinforcement works together due to bond.**

Bond → defined by the bond strength,  $f_b$

→ is produced by

- a) **adhesion between concrete and steel  $\approx 10\%$**
- b) friction between reinforcement & concrete
- c) clenching of concrete between bar ribs



The cube can not be moved because it is stuck on the metal plate

## Anchorage / Ancorarea

**Concrete and reinforcement works together due to bond.**

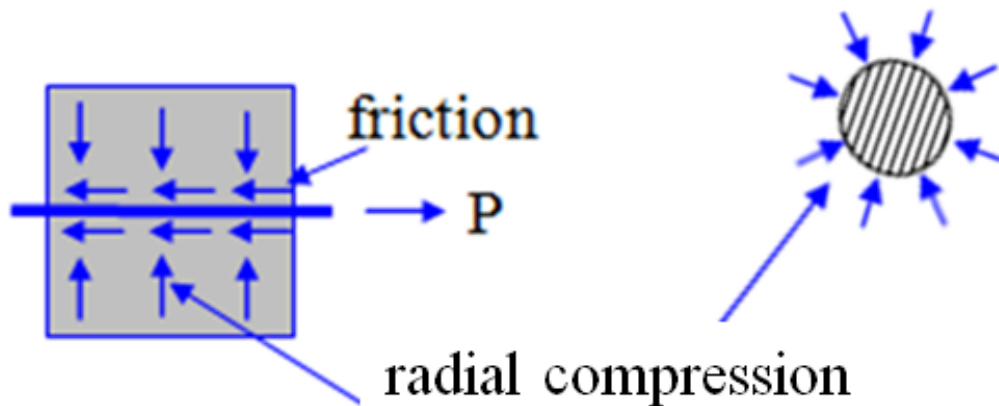
Bond → defined by the bond strength,  $f_b$

→ is produced by

a) adhesion between concrete and steel  $\approx 10\%$

**b) friction between reinforcement & concrete  $\approx 20\%$**

c) clenching of concrete between bar ribs



- fresh concrete is shrinking
- radial compression is produced
- moving bar entail friction

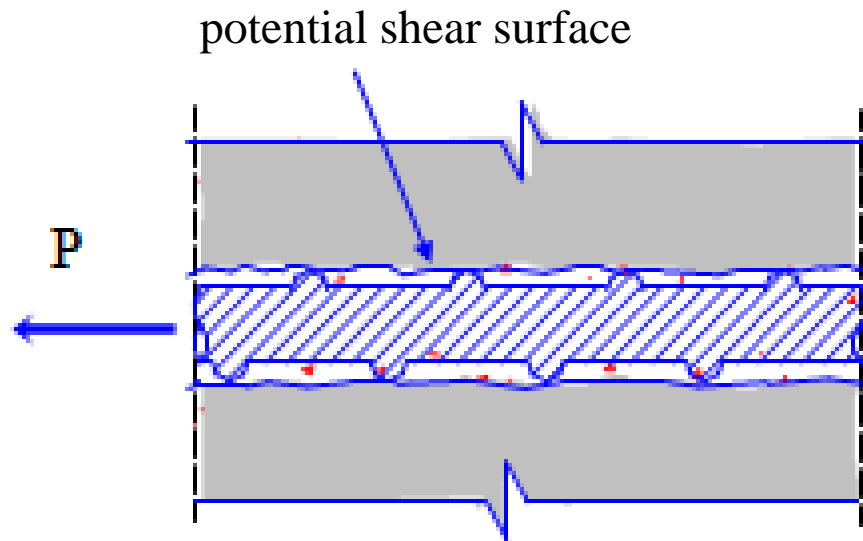
## Anchorage / Ancorarea

**Concrete and reinforcement works together due to bond.**

Bond → defined by the bond strength,  $f_b$

→ is produced by

- adhesion between concrete and steel  $\approx 10\%$
- friction between reinforcement & concrete  $\approx 20\%$
- clenching of concrete between bar ribs  $\approx 70\%$**



Reinforcing bars are: → easy to pull-out the bar

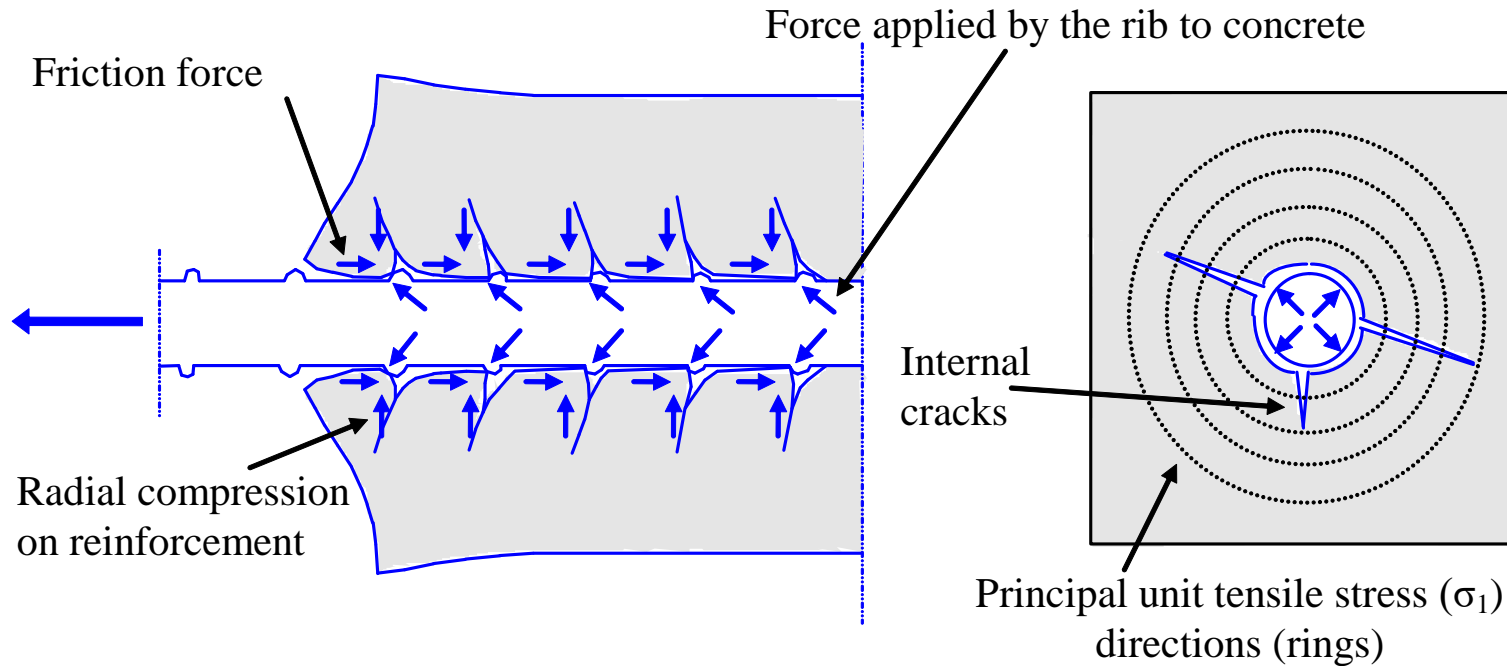
- plain: OB37 (RO)
- **ribbed: PC52 (RO), S500 (EU)**

- concrete must be sheared on a cylindrical surface to pull-out the bar.
- will be difficult to produce concrete shear



## Anchorage / Ancorarea

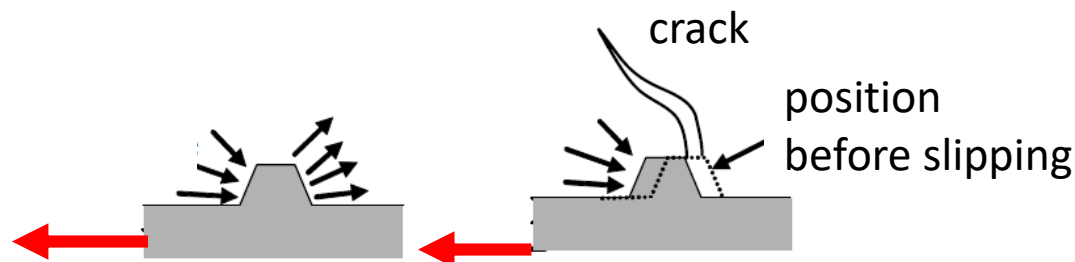
## Bond model for a reinforcement with periodic profile



a) internal cracking of concrete

b) concrete splitting  $\sigma_1 = f_{ct}$ 

(dislocation of a relative large amount of concrete)

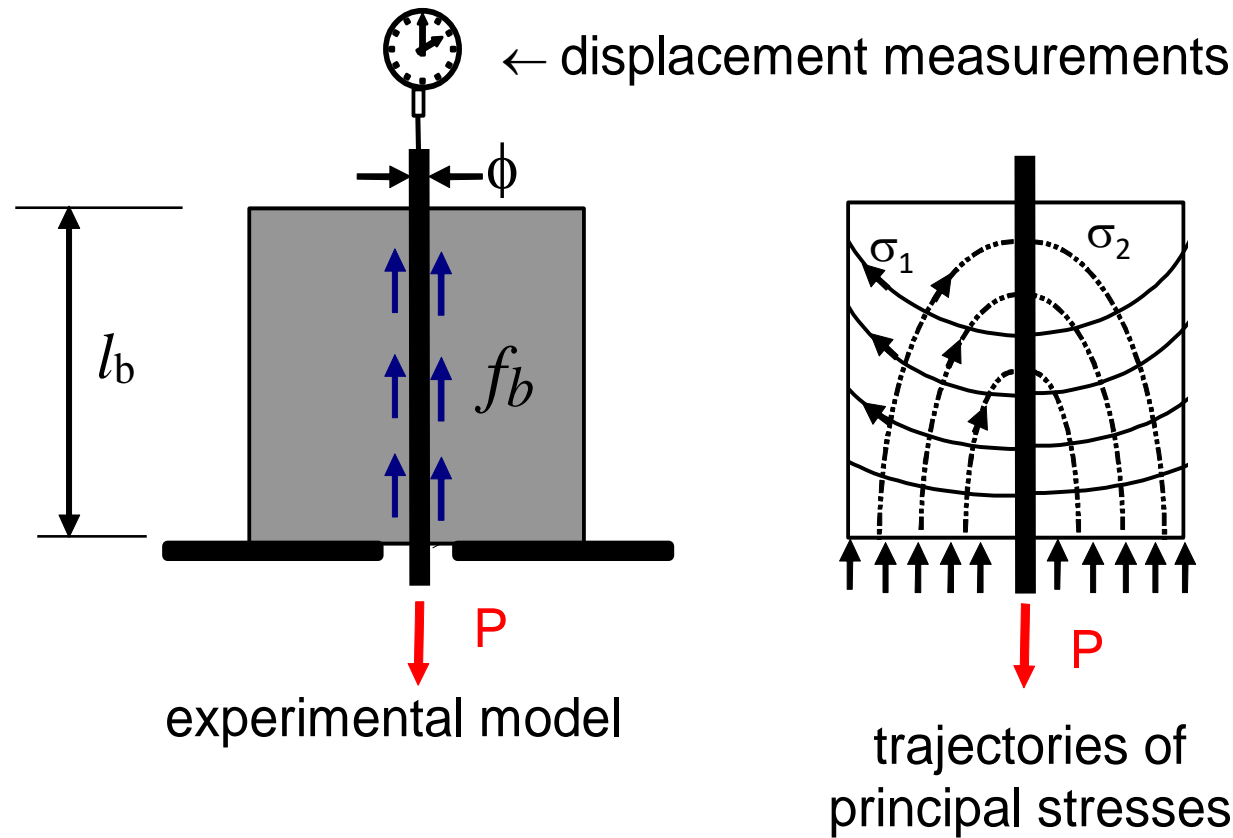


c) rib detail

## Anchorage / Ancorarea

## Bond stress is obtained by pull-out test

- Failure mode → Pulling out of the bar (plane bar)  
 → Cracking of concrete (ribbed bar)



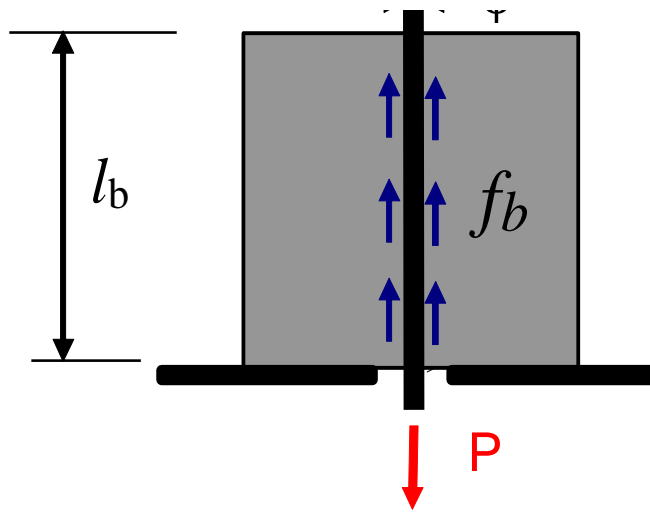
$$\sigma_1 \rightarrow f_{ct}$$

## Anchorage / Ancorarea

**Bond stress is obtained by pull-out test**

## Bond failure

- bar sliding for plain bars
- concrete cracking, even splitting in 2 or 3 pieces for ribbed bar



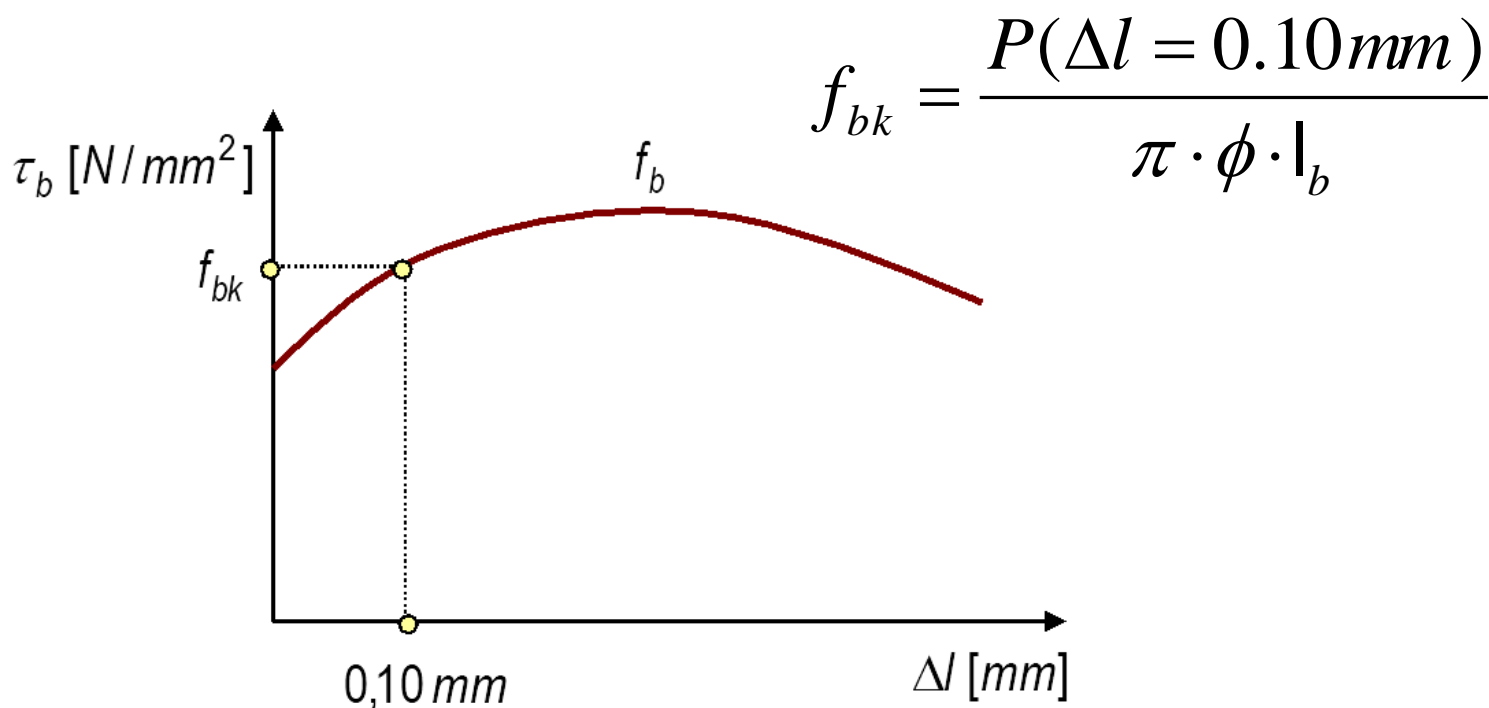
$$f_b = \frac{P}{\pi \cdot \phi \cdot l_b}$$

## Anchorage / Ancorarea

**Bond stress is obtained by pull-out test**

## Bond failure

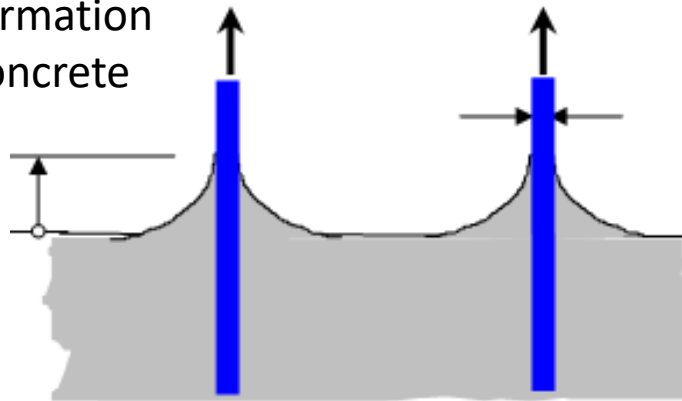
- bar sliding for plain bars
- concrete cracking, even splitting in 2 or 3 pieces for ribbed bar



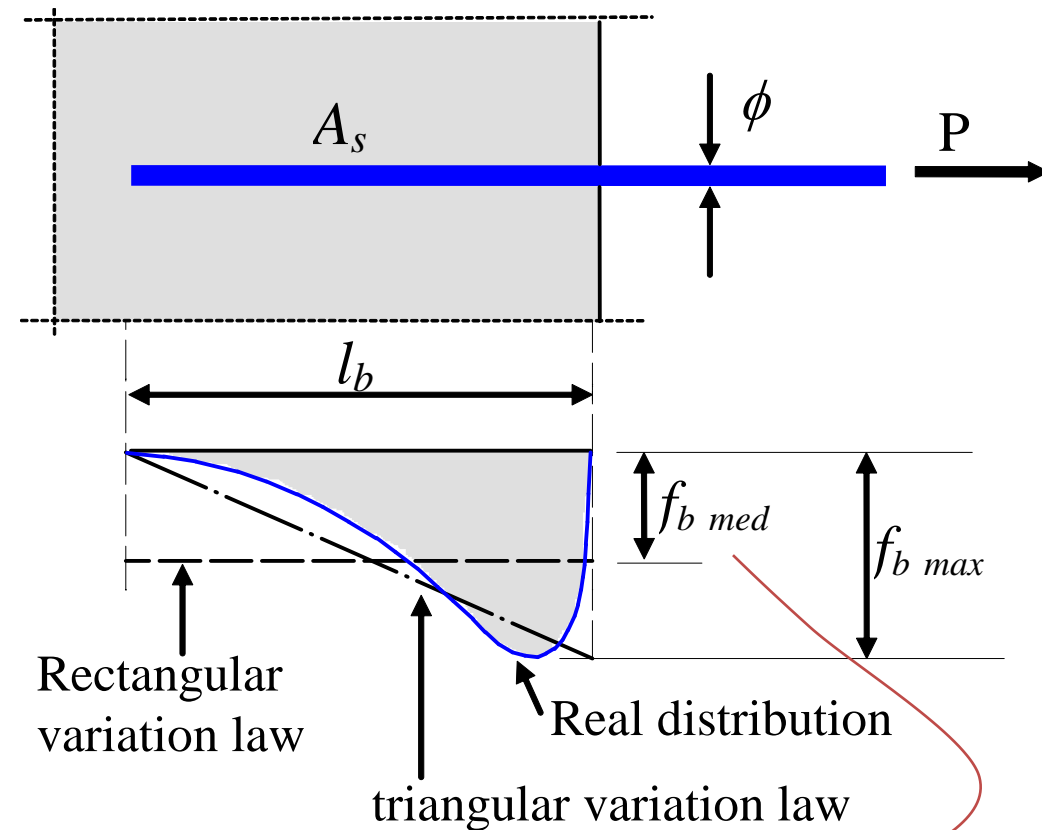
## Anchorage / Ancorarea

## Unit bond stress distribution in transversal and longitudinal directions

local

deformation  
of concrete

action range  $r = (10 \dots 15)\phi$   
(influence zone)

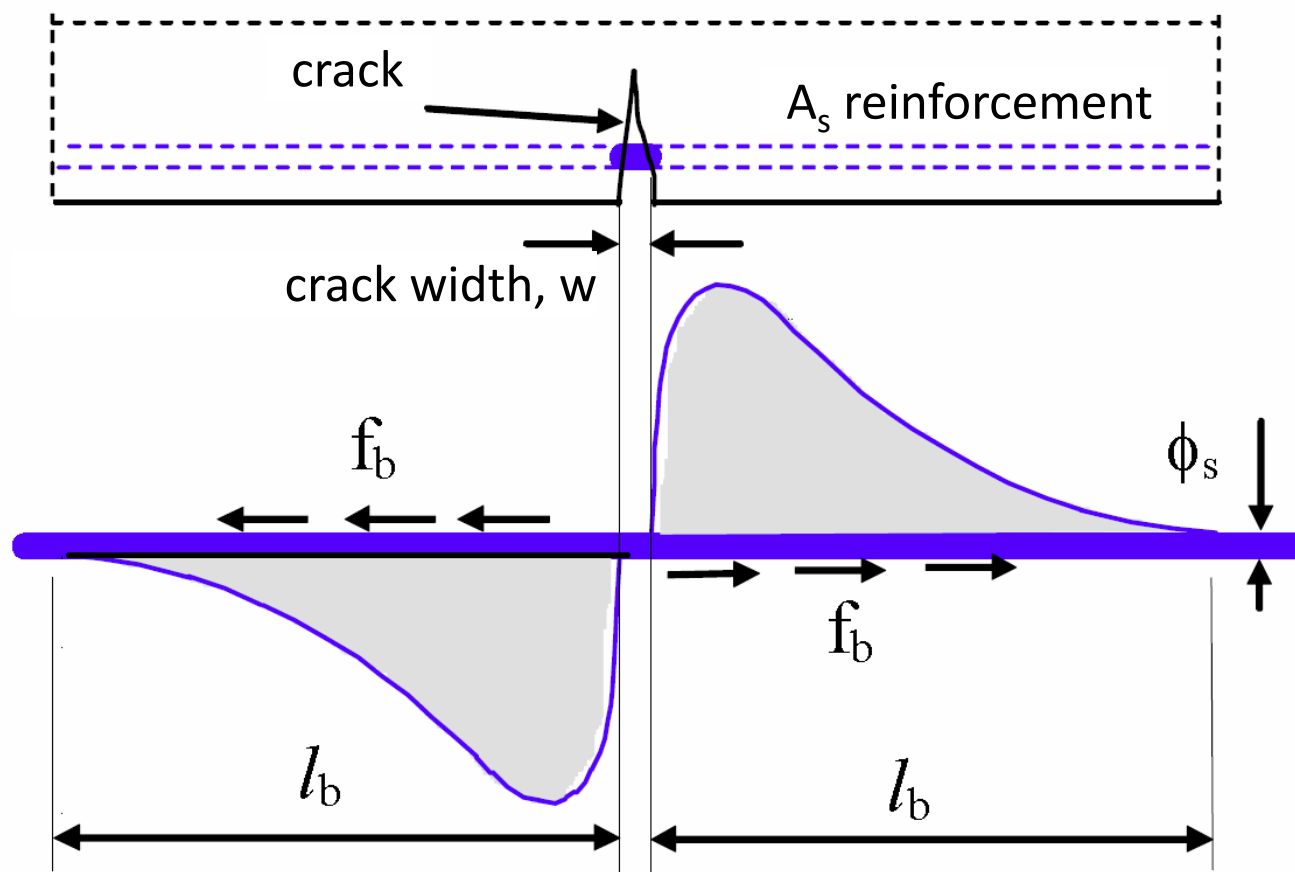


$$f_{b \text{ med}} = \frac{P}{\pi \cdot \phi \cdot l_b}$$

1. It is advisable to avoid overlapping of influence zones
2. Usually, the overlapping of influence zones can not be avoided

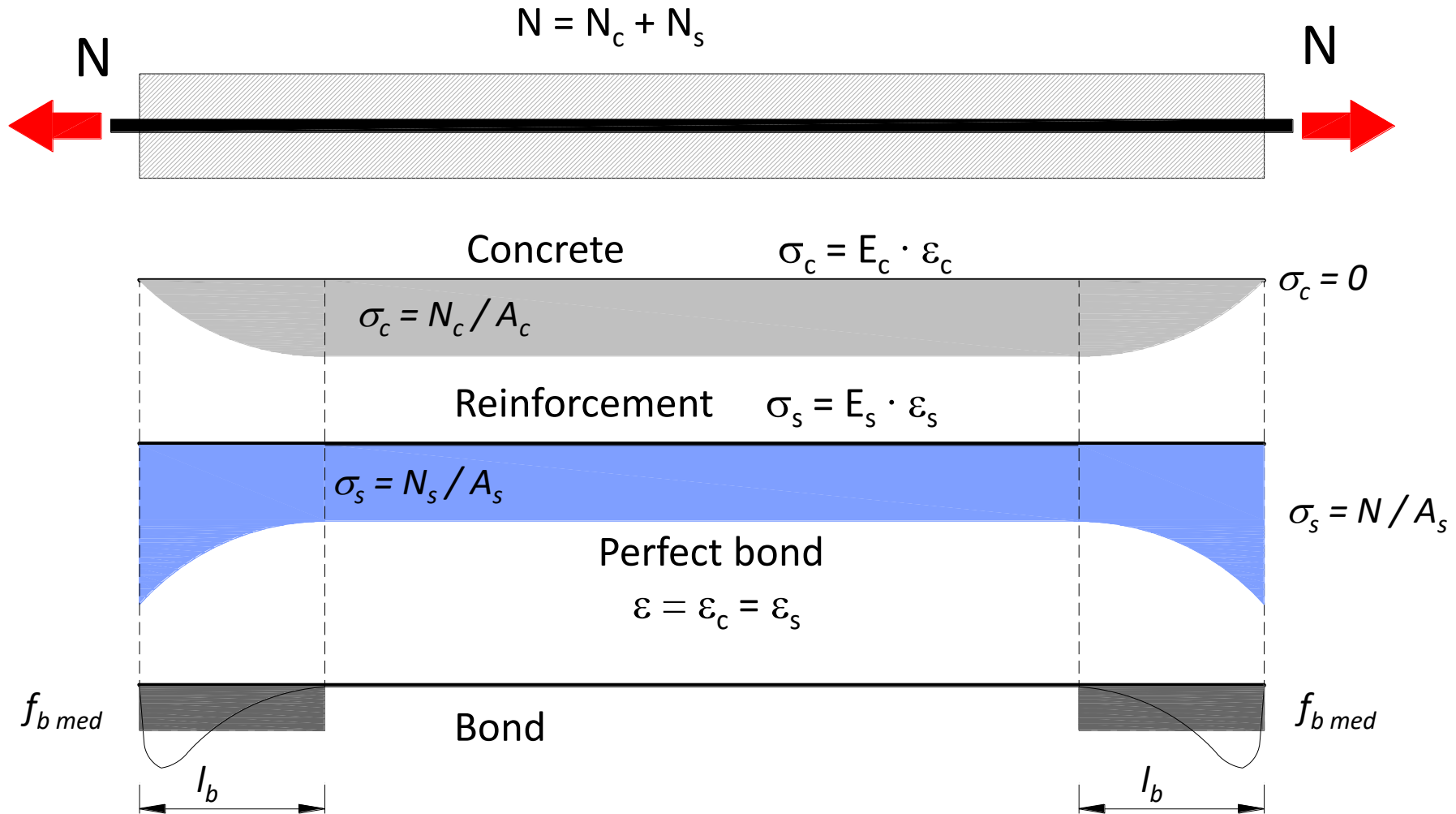
## Anchorage / Ancorarea

## Unit bond stress distribution in a beam, near a crack



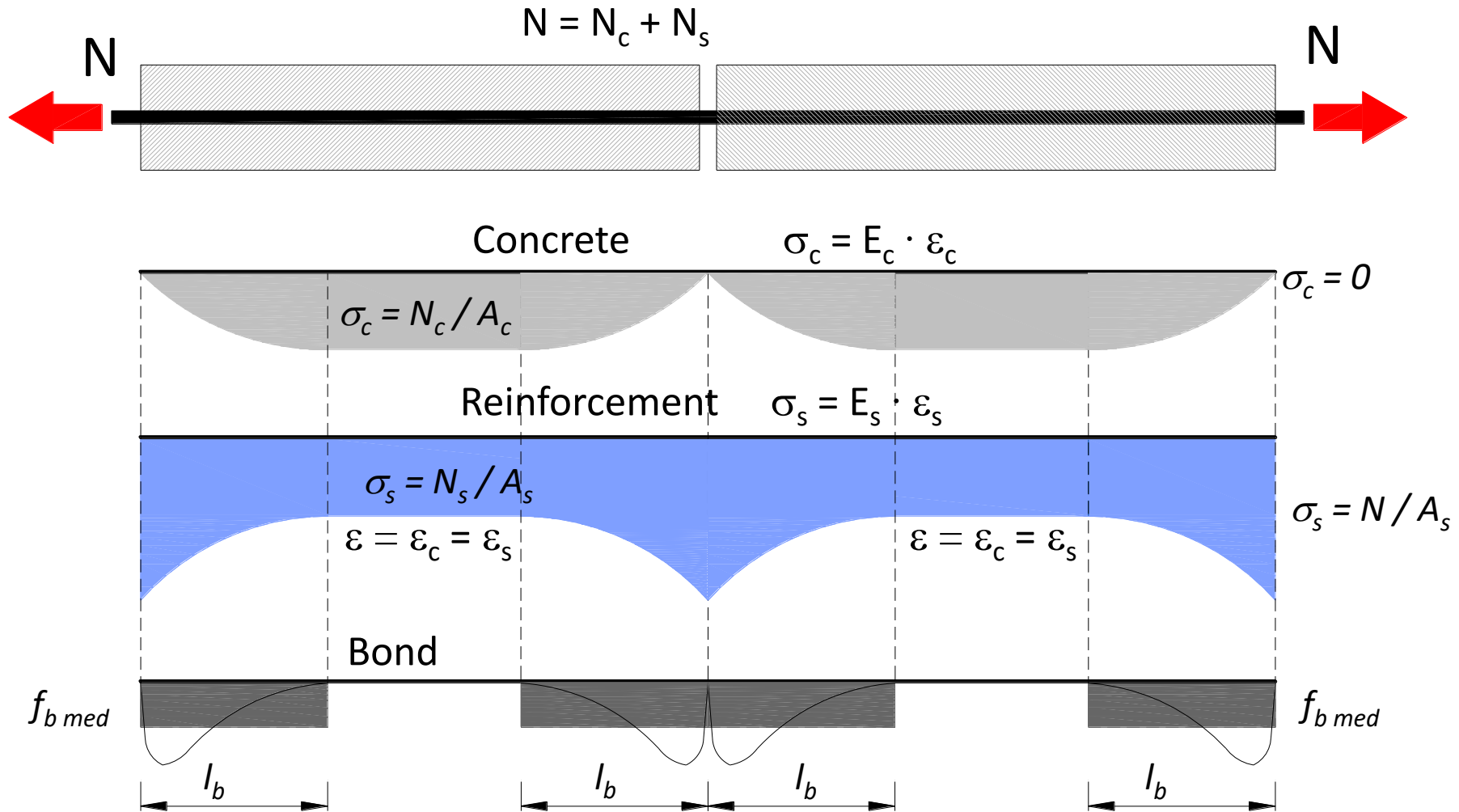
## Anchorage / Ancorarea

## Behavior of reinforcement embedded in concrete for centric tension



## Anchorage / Ancorarea

## Behavior of reinforcement embedded in concrete for centric tension





## Anchorage / Ancorarea

**Necessary anchorage length**  $l_b$   $\rightarrow$  ensure stress transmission from reinforcement to concrete through bond on this length

Rational failure condition: bond failure to be produce simultaneously with reinforcement yielding ( $\sigma_{sd} = f_{yd}$ )

$$N_c = N_s$$

$$\pi \cdot \phi \cdot l_b \cdot f_{bmed} = \frac{\pi \cdot \phi^2}{4} f_y \quad \rightarrow \quad l_b = \frac{\phi \cdot f_y}{4 \cdot f_{bmed}}$$

In conformity to EC2:

$$l_{b,rqd} = \frac{\phi \cdot \sigma_{sd}}{4 \cdot f_{bd}}$$

where  $l_{bd} = \alpha_1 \alpha_2 \alpha_3 \alpha_4 \alpha_5 l_{b,rqd} \geq l_{b,min}$

At the limit:

$$l_{b,rqd} = \frac{\phi \cdot f_{yd}}{4 \cdot f_{bd}}$$

## Anchorage / Ancorarea

Table 8.2: Values of  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$ ,  $\alpha_4$  and  $\alpha_5$  coefficients

Influencing factor	Type of anchorage	Reinforcement bar	
		In tension	In compression
Shape of bars	Straight	$\alpha_1 = 1,0$	$\alpha_1 = 1,0$
	Other than straight (see Figure 8.1 (b), (c) and (d))	$\alpha_1 = 0,7$ if $c_d > 3\phi$ otherwise $\alpha_1 = 1,0$ (see Figure 8.3 for values of $c_d$ )	$\alpha_1 = 1,0$
Concrete cover	Straight	$\alpha_2 = 1 - 0,15 (c_d - \phi) / \phi$ $\geq 0,7$ $\leq 1,0$	$\alpha_2 = 1,0$
	Other than straight (see Figure 8.1 (b), (c) and (d))	$\alpha_2 = 1 - 0,15 (c_d - 3\phi) / \phi$ $\geq 0,7$ $\leq 1,0$ (see Figure 8.3 for values of $c_d$ )	$\alpha_2 = 1,0$
Confinement by transverse reinforcement not welded to main reinforcement	All types	$\alpha_3 = 1 - K\lambda$ $\geq 0,7$ $\leq 1,0$	$\alpha_3 = 1,0$
Confinement by welded transverse reinforcement*	All types, position and size as specified in Figure 8.1 (e)	$\alpha_4 = 0,7$	$\alpha_4 = 0,7$
Confinement by transverse pressure	All types	$\alpha_5 = 1 - 0,04p$ $\geq 0,7$ $\leq 1,0$	-

$$l_{bd} = \alpha_1 \alpha_2 \alpha_3 \alpha_4 \alpha_5 l_{b,rqd} \geq l_{b,min}$$

## Anchorage / Ancorarea

$\alpha_1$  - form of the bars assuming adequate cover

$\alpha_2$  - concrete minimum cover

$\alpha_3$  - confinement by transverse reinforcement

$\alpha_4$  - influence of one or more welded transverse bars ( $\phi_t > 0,6\phi$ ) along the design anchorage length

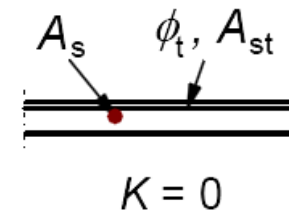
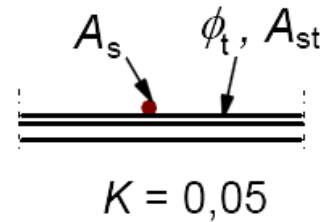
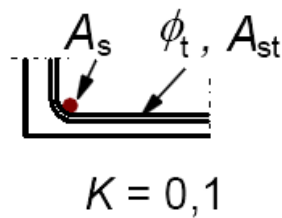
$\alpha_5$  - effect of the pressure transverse to the plane of splitting along the design anchorage length

$$\alpha_2 \alpha_3 \alpha_5 \geq 0,7$$

$$l_{bd} = \alpha_1 \alpha_2 \alpha_3 \alpha_4 \alpha_5 l_{b,rqd} \geq l_{b,min}$$

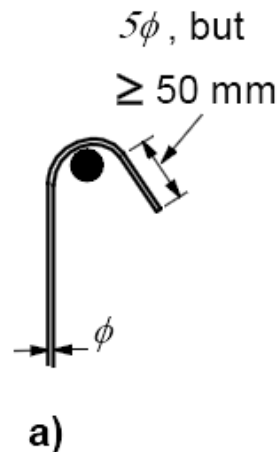
## Anchorage / Ancorarea

## Effects of non-welded reinforcements

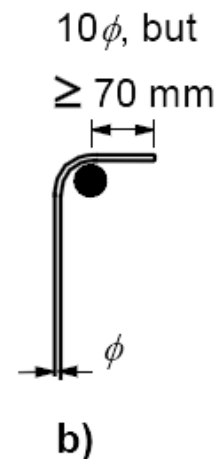


## Anchorage of links and shear reinforcement

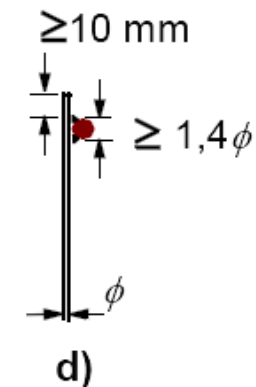
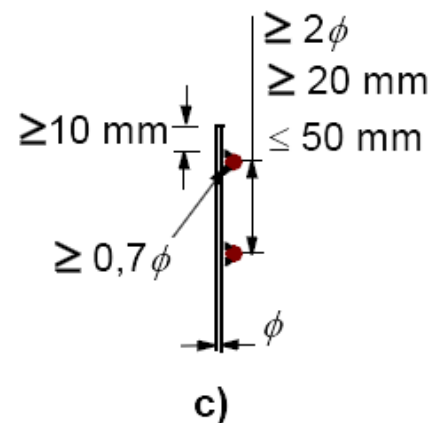
hook



bend



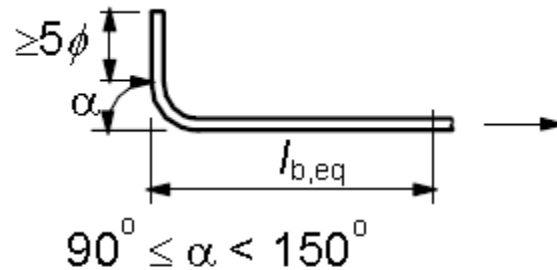
Welded transverse reinforcement



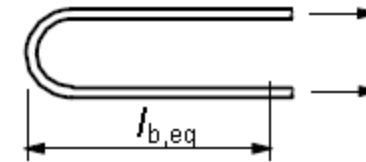
## Anchorage / Ancorarea

Simplification:

$$l_{bd} = \alpha_1 l_{b,rqd} \quad \text{- for shapes shown in Figure 8.1b to 8.1d}$$



b) Equivalent anchorage length for standard bend



d) Equivalent anchorage length for standard loop

Table 8.2: Values of  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$ ,  $\alpha_4$  and  $\alpha_5$  coefficients

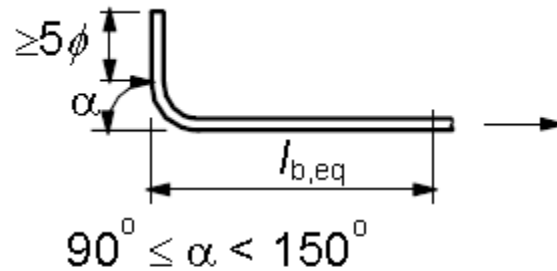
Influencing factor	Type of anchorage	Reinforcement bar	
		In tension	In compression
Shape of bars	Straight	$\alpha_1 = 1,0$	$\alpha_1 = 1,0$
	Other than straight (see Figure 8.1 (b), (c) and (d))	$\alpha_1 = 0,7$ if $c_d > 3\phi$ otherwise $\alpha_1 = 1,0$ (see Figure 8.3 for values of $c_d$ )	$\alpha_1 = 1,0$

## Anchorage / Ancorarea

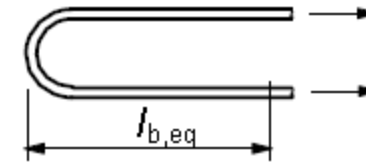
Simplification:

$$l_{bd} = \alpha_1 l_{b,rqd}$$

- for shapes shown in Figure 8.1b to 8.1d

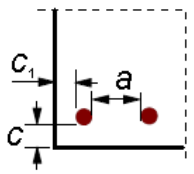
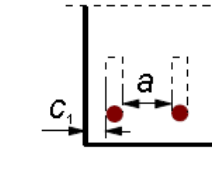
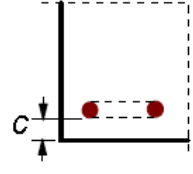


b) Equivalent anchorage length for standard bend



d) Equivalent anchorage length for standard loop

Table 8.2: Values of  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$ ,  $\alpha_4$  and  $\alpha_5$  coefficients

Type of anchorage	Reinforcement bar			
	In tension	In compression		
 <p>a) Straight bars <math>c_d = \min(a/2, c_1, c)</math></p>	 <p>b) Bent or hooked bars <math>c_d = \min(a/2, c_1)</math></p>	 <p>c) Looped bars <math>c_d = c</math></p>	$\alpha_1 = 1,0$	$\alpha_1 = 1,0$
(see Figure 8.3 for values of $c_d$ )			$\alpha_1 = 0,7$ if $c_d > 3\phi$ otherwise $\alpha_1 = 1,0$	$\alpha_1 = 1,0$

## Anchorage / Ancorarea

$$f_{bd} = 2.25 \cdot \eta_1 \cdot \eta_2 \cdot f_{ctd} \rightarrow \text{design value of the ultimate bond stress}$$

where:

$\eta_1$  - is a coefficient related to the quality of the bond condition and the position of the bar during concreting  
 = 1.0  $\rightarrow$  when 'good' conditions are obtained  
 = 0.7  $\rightarrow$  for all other cases

$\eta_2$  - is related to the bar diameter  
 = 1.0 pt  $\phi \leq 32$  mm  
 =  $(132 - \phi) / 100$  pt  $\phi > 32$  mm

$f_{ctd}$  - design tensile strength of concrete

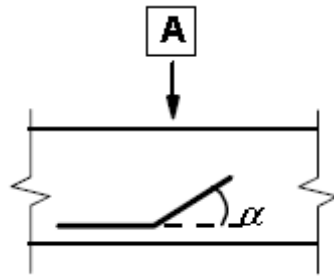
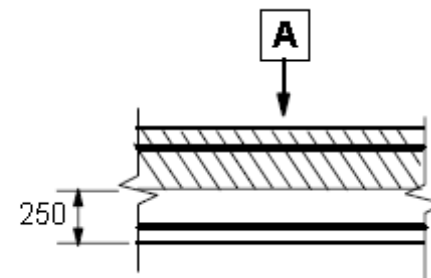
$$l_{b,rqd} = \frac{\phi \cdot f_{yd}}{4 \cdot f_{bd}}$$

$$l_{bd} = \alpha_1 \alpha_2 \alpha_3 \alpha_4 \alpha_5 l_{b,rqd} \geq l_{b,min}$$

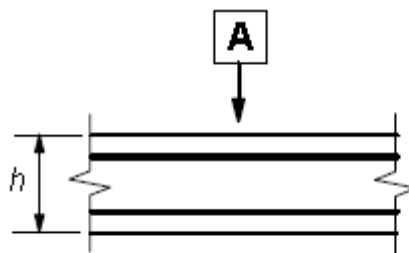
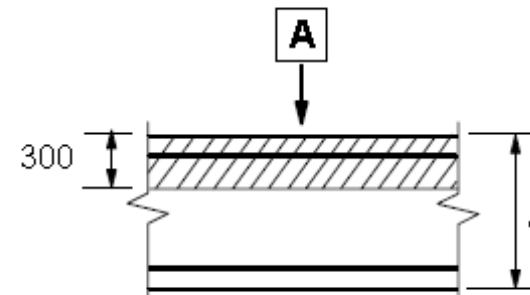
## Anchorage / Ancorarea

$$f_{bd} = 2.25 \cdot \eta_1 \cdot \eta_2 \cdot f_{ctd} \rightarrow \text{design value of the ultimate bond stress}$$

Bond conditions:

a)  $45^\circ \leq \alpha \leq 90^\circ$ c)  $h > 250 \text{ mm}$ 

A Direction of concreting

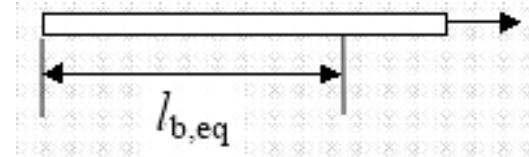
b)  $h \leq 250 \text{ mm}$ d)  $h > 600 \text{ mm}$ a) & b) 'good' bond conditions  
for all barsc) & d) unhatched zone – 'good' bond conditions  
hatched zone – 'poor' bond conditions



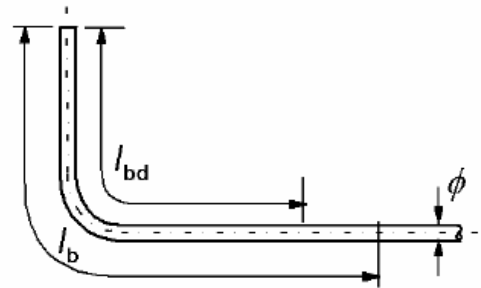
## Anchorage / Ancorarea

Longitudinal reinforcement bars can be anchored to through the following forms:

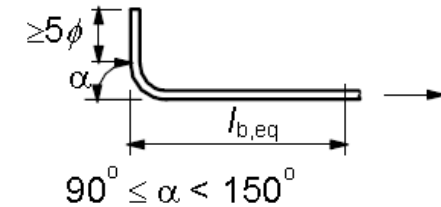
### 1. Strait ends



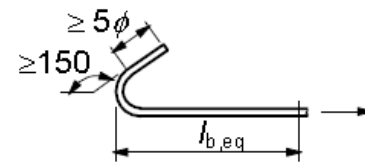
### 2. Bent ends



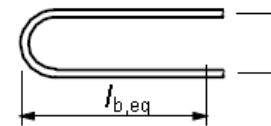
a) Basic tension anchorage length,  $l_b$ , for any shape measured along the centreline



b) Equivalent anchorage length for standard bend



c) Equivalent anchorage length for standard hook

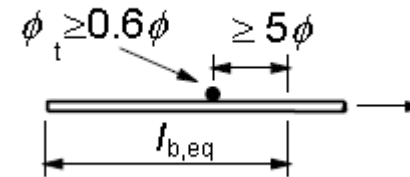


d) Equivalent anchorage length for standard loop

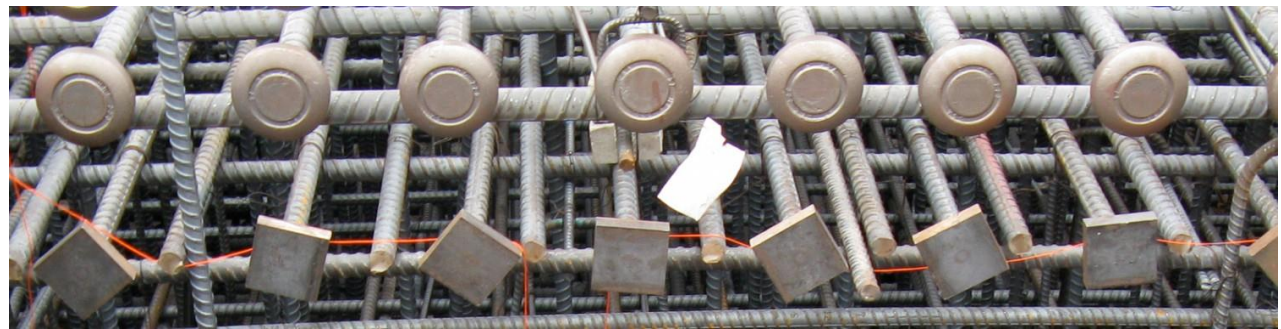
## Anchorage / Ancorarea

Longitudinal reinforcement bars can be anchored to through the following forms:

### 3. Welded transverse bar



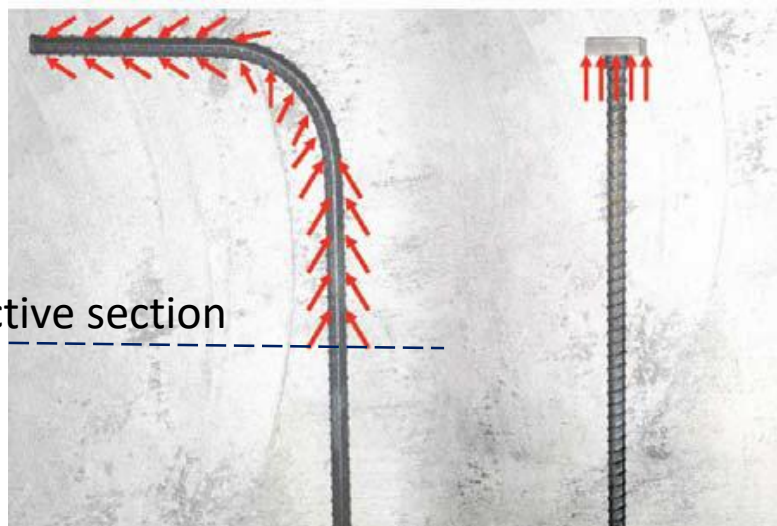
### 4. Special-end anchorage (headed reinforcement)



## Anchorage / Ancorarea

### 4. Special-end anchorage (headed reinforcement)

- Transfer through concentrated stresses eliminates the need of anchorage length, without using bond
- The total length of the bar can be used
- Reducing agglomeration of reinforcements → element size reduction
- Stiff anchorage at shear reinforcement reduce shear strains, thus reducing shear crack width



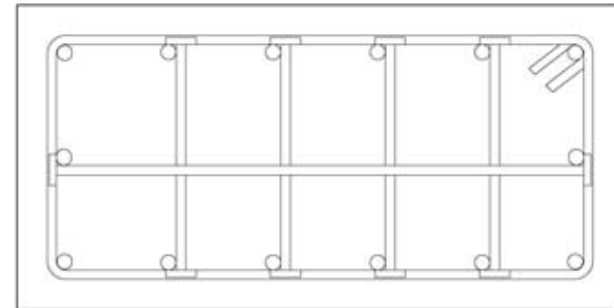
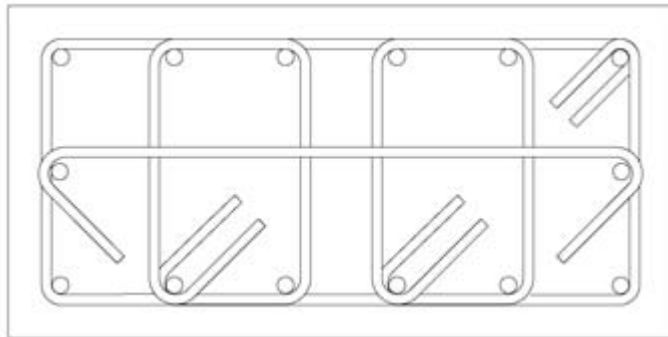
Stress distribution



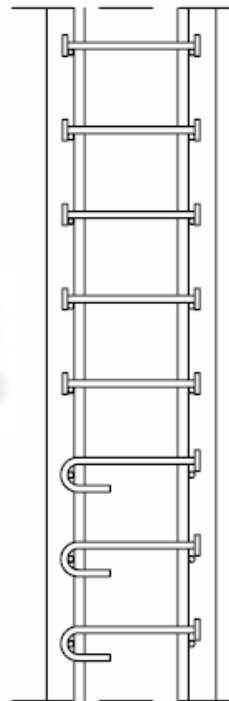
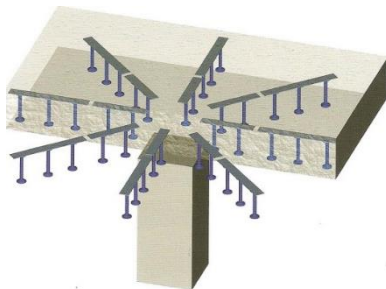
Position of the active section

## Anchorage / Ancorarea

## 4. Special-end anchorage (headed reinforcement)

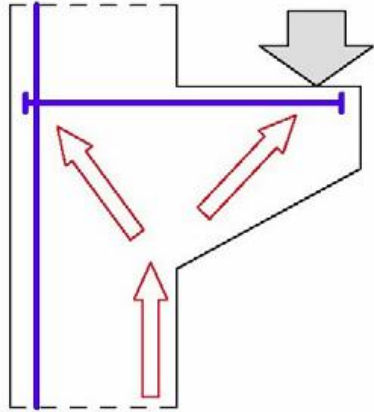


- Easy and fast to install
- No hooks or bends
- Costs ???

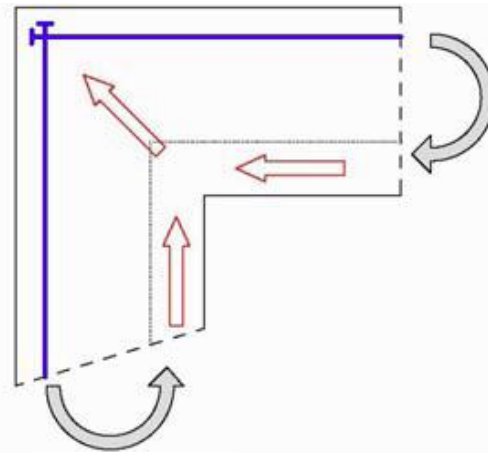


## Anchorage / Ancorarea

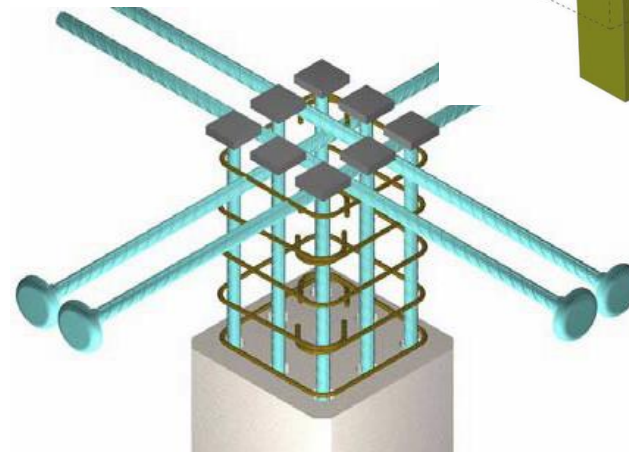
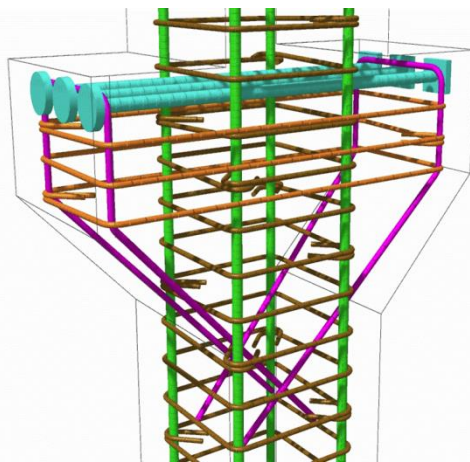
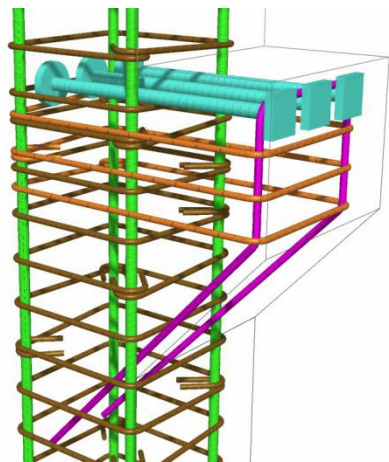
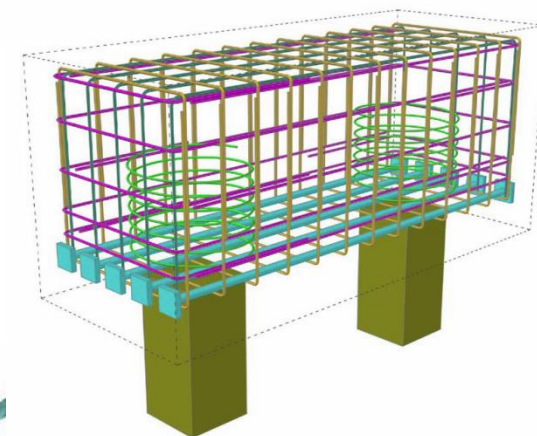
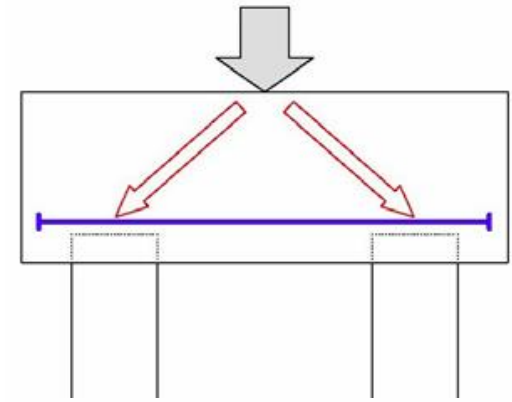
## 4. Special-end anchorage (headed reinforcement)



Cantilever



Column

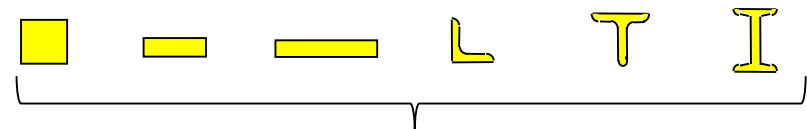
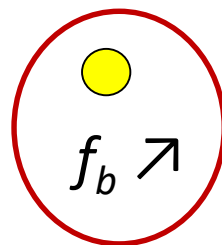


(hrc.com)

## Anchorage / Ancorarea

**Bond strength depends on:**

- |  |                              |  |
|--|------------------------------|--|
| Concrete quality                                   | $C \nearrow$                 | $\Rightarrow f_b \nearrow$             |
| - Cement dosage                                    | $\text{Cem} \nearrow$        | $\Rightarrow f_b \nearrow$             |
| - Water – cement ratio                             | $W/\text{Cem} \nearrow$      | $\Rightarrow f_b \searrow$             |
| - Compaction                                       | $\text{Compaction} \nearrow$ | $\Rightarrow f_b \nearrow$             |
| - Position of the reinforcement during the casting |                              |  |
|  | for horizontal bars          | $\Rightarrow f_b \searrow$ (air voids) |
|  | for vertical bars            | $\Rightarrow f_b \nearrow$             |
| - Shape of the reinforcement cross-section         |                              |  |



- peaks in stress distribution
- weak compaction of concrete

## Anchorage / Ancorarea

## Bond strength depends on:

- Diameter of the bars

$\phi \nearrow$

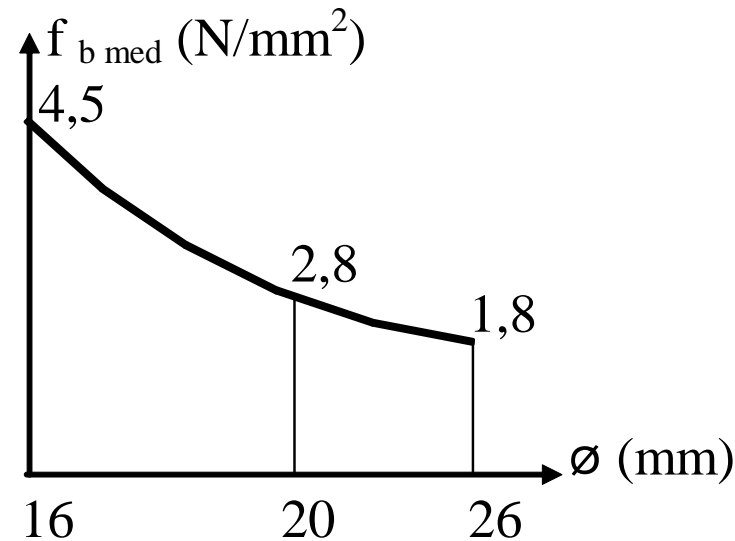
$\Rightarrow f_b \searrow$

Ex:

$1\phi 16 = 4\phi ?$

$f_{b,\phi 16} = ? \text{ MPa}$

$f_{b,\phi ?} = ? \text{ MPa}$



- Concrete cover

C. cover  $\searrow$

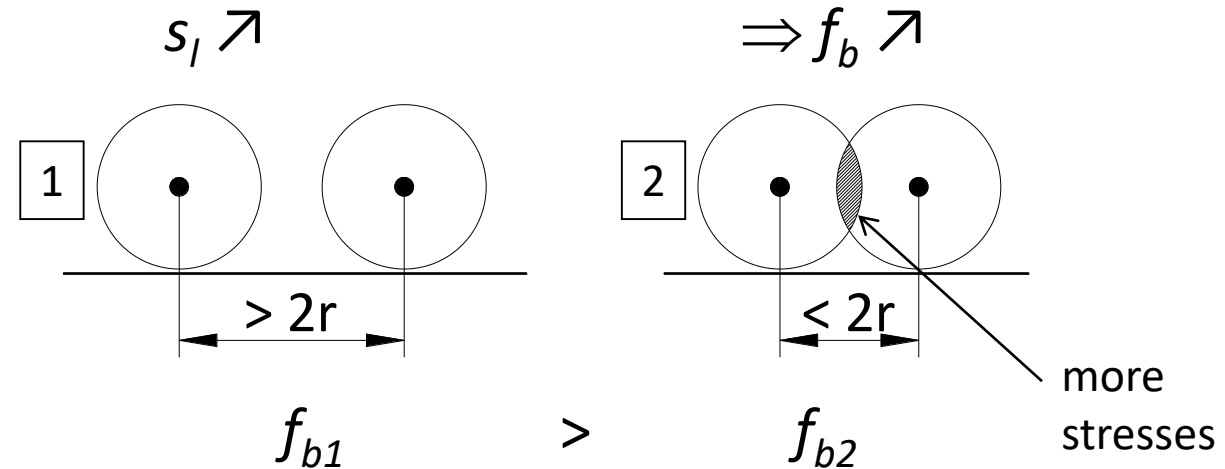
$\Rightarrow f_b \searrow$

radial compression  $\searrow$

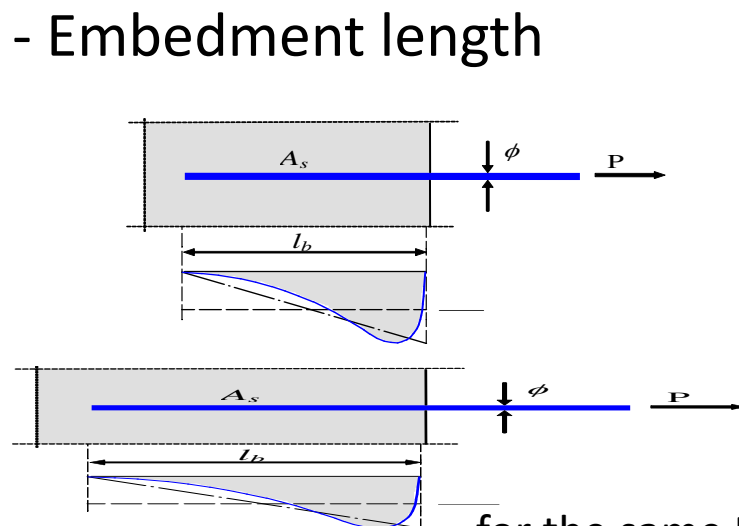
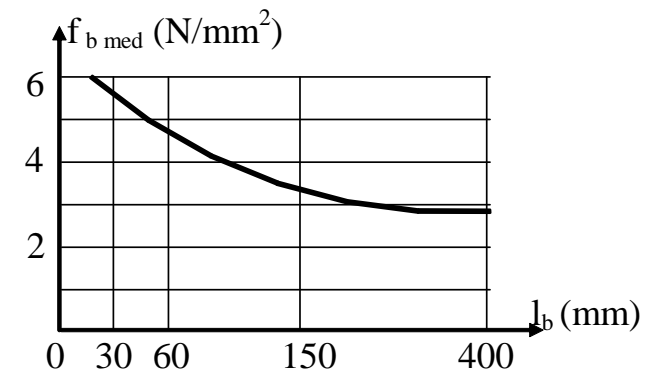
## Anchorage / Ancorarea

## Bond strength depends on:

- Bar spacing



- Embedment length

for the same  $P$ : diagram will be elongated therefore  $f_{b\ med} \searrow$ 

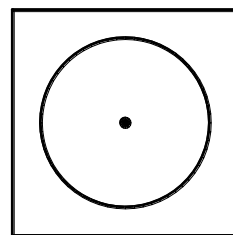
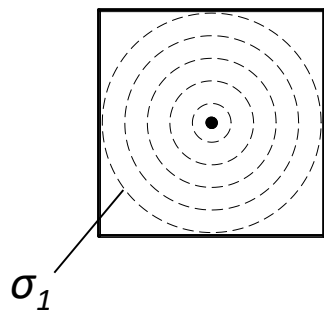
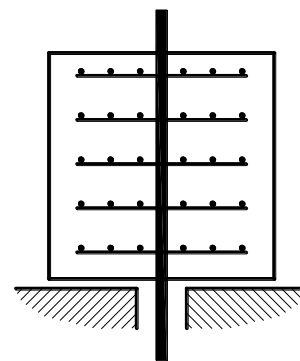
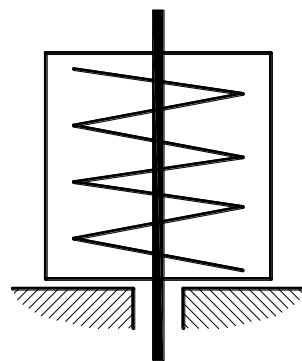
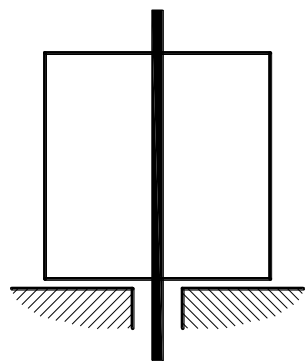


## Anchorage / Ancorarea

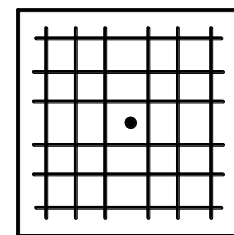
## Bond strength depends on:

- Transversal reinforcement prevents (transversal) deformation

$\Rightarrow f_b \nearrow$



Spiral  
reinforcement



Welded  
wire

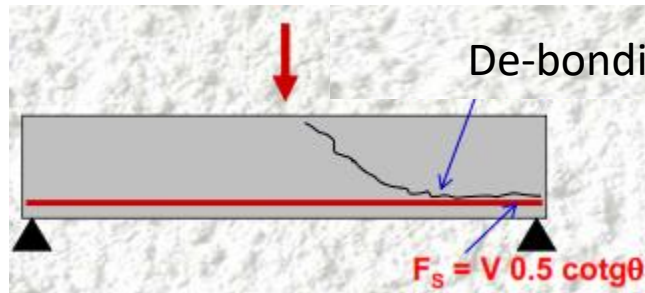
1

2

$$f_{b1} < f_{b2}$$

## Anchorage / Ancorarea

## Why bars should be anchored ?



**CORRECT DETAILING**

## Summary:

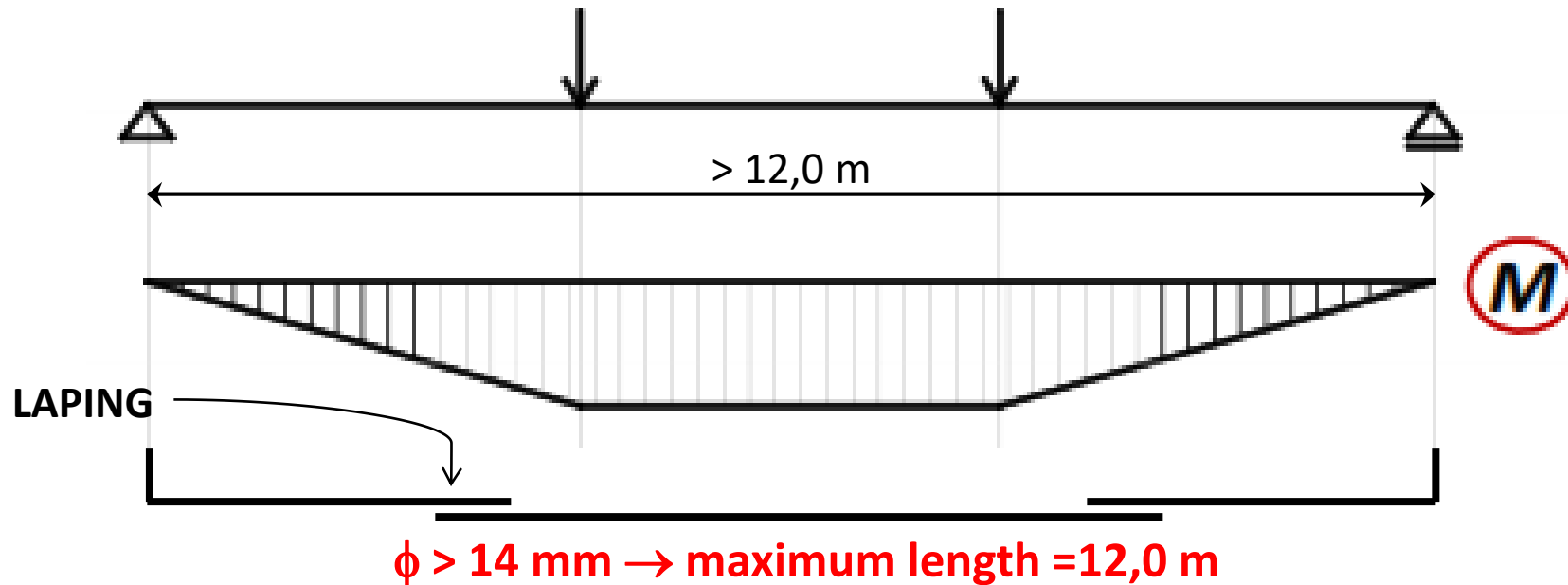
Anchorage of the bars must be realized to ensure:

- good transfer of reinforcement tensile force to concrete
- avoid longitudinal cracks and concrete splitting.

For this reason the following requirements will be fulfilled:

- the minimum spacing of the bars
- anchorage of the bars
- disposing transversal bars (welded or non-welded), if necessary
- the sufficient concrete cover

## LAPPING OF BARS

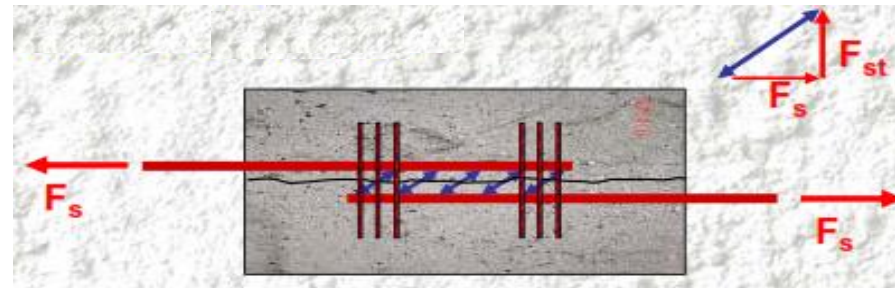
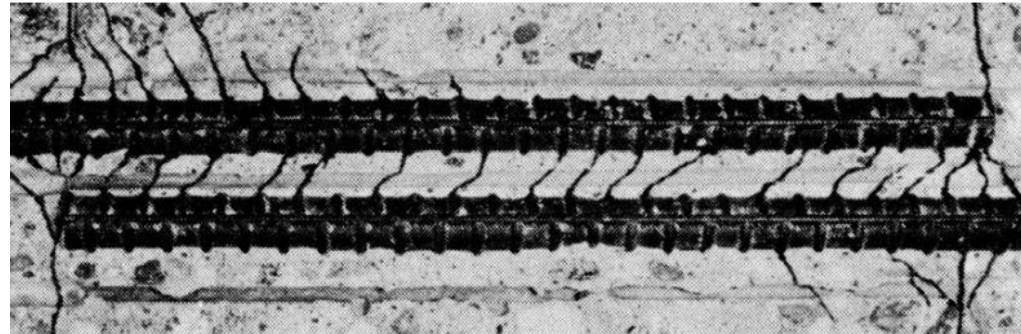


Forces are transmitted from one bar to another by:

- lapping of bars provided with or without bends or hooks;
- welding;
- mechanical devices.

Connection between bars should normally be staggered and not located in areas of high moments/forces (e.g. supports, plastic hinges)

## LAPPING OF BARS



THE FLOW OF FORCE:

reinforcement – bond – concrete – bond – reinforcement

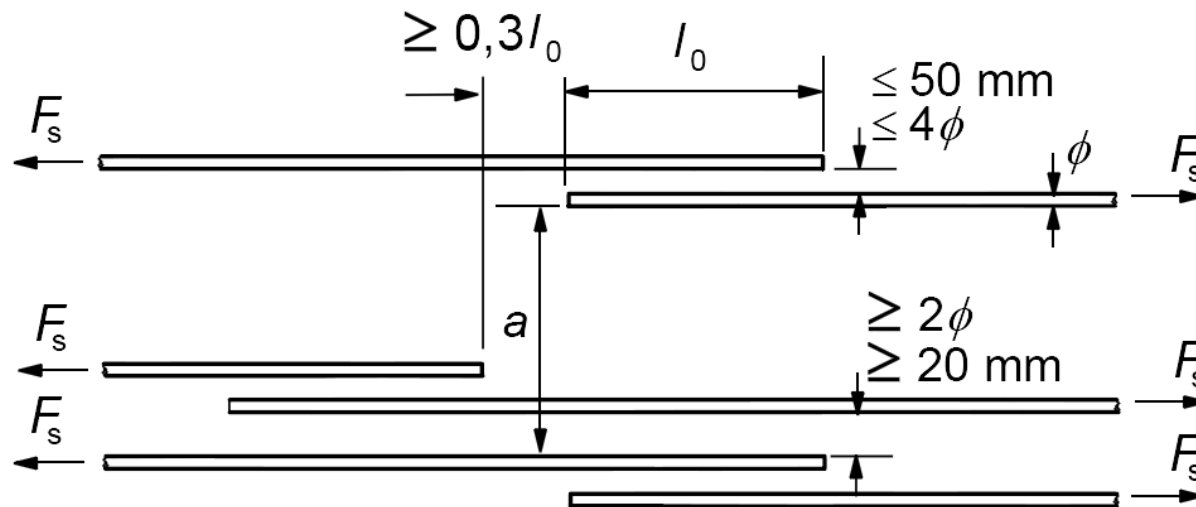


Consequence of this flow is the tensile force in concrete



Transverse reinforcement is required

## Arrangement of lapped bars



$$l_0 = \alpha_1 \cdot \alpha_2 \cdot \alpha_3 \cdot \alpha_5 \cdot \alpha_6 \cdot l_{b,rqd} \geq l_{0,min} \rightarrow \text{design lap length}$$

$\alpha_6 \rightarrow$

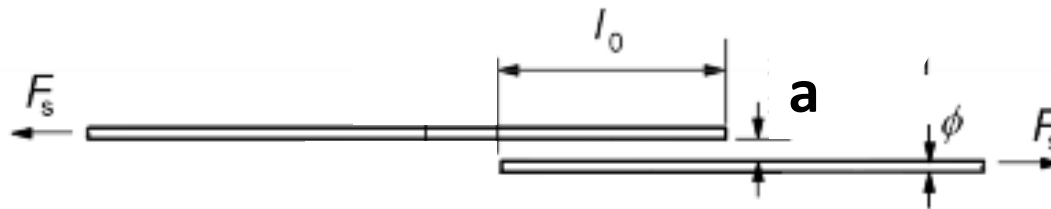
Percentage of lapped bars relative to the total cross-section area	< 25%	33%	50%	>50%
$\alpha_6$	1	1,15	1,4	1,5

Note: Intermediate values may be determined by interpolation.

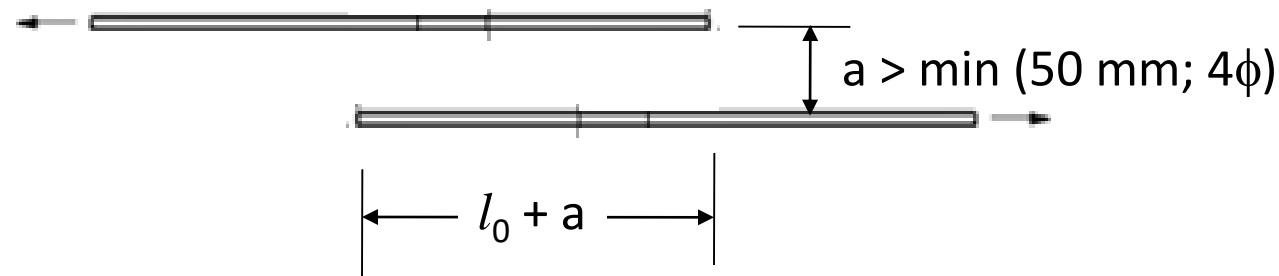
All bars in compression and secondary (distribution) reinforcement may be lapped in one section.

## Arrangement of lapped bars

### Clear distance between lapped bars

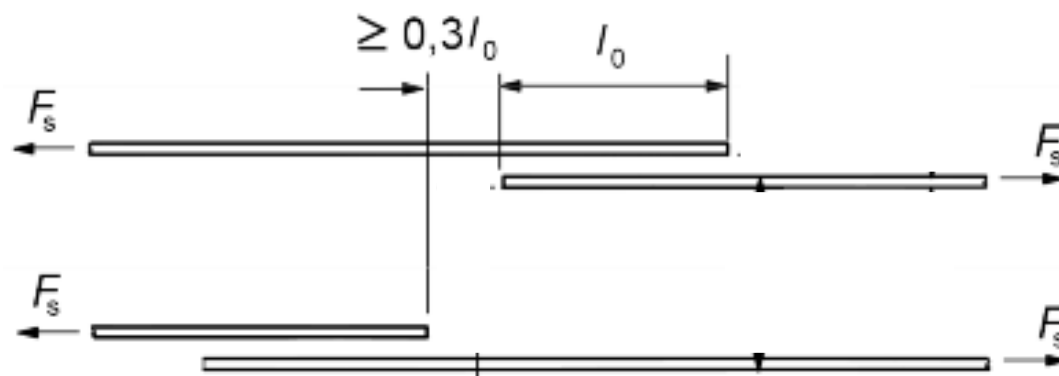


$a \leq \min(50 \text{ mm}; 4\phi)$  otherwise  $l_0$  should be increased by  $a$

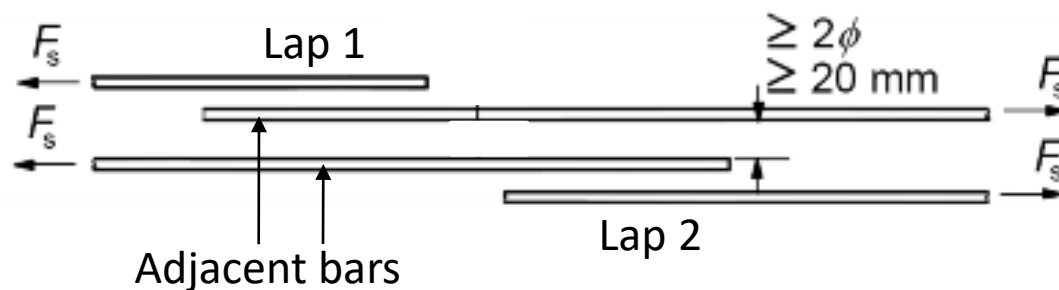


## Arrangement of lapped bars

### Longitudinal distance between two adjacent laps



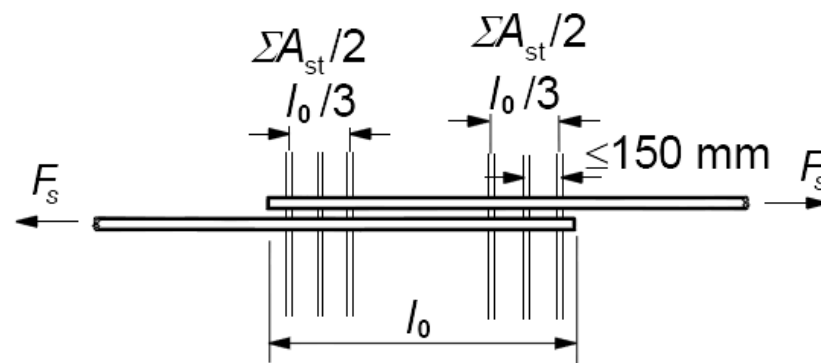
### Clear distance between adjacent bars in case of adjacent laps





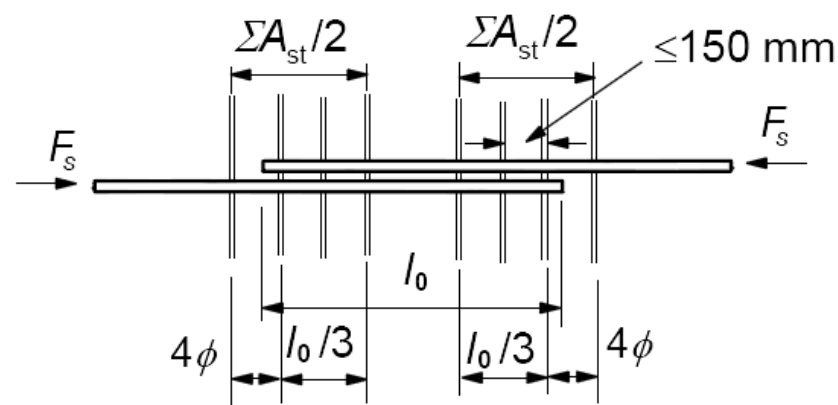
## Transverse reinforcement in the lap zone

→ is required in the lap zone to resist transverse tension forces



a) bars in tension

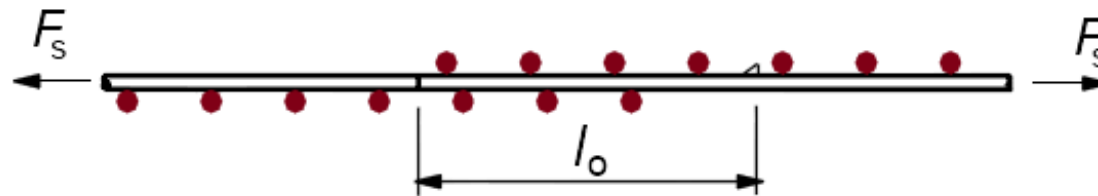
$$\Sigma A_{st} \geq 1.0 A_s$$



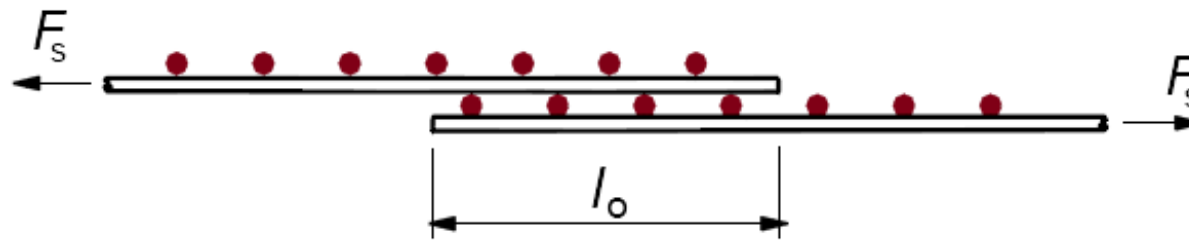
b) bars in compression

→ + 1 transversal bar

## Laps for welded mesh fabrics made of ribbed wires reinforcement



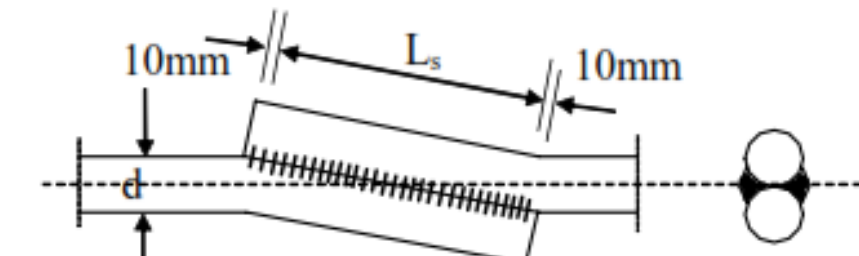
a) intermeshed fabric (longitudinal section)



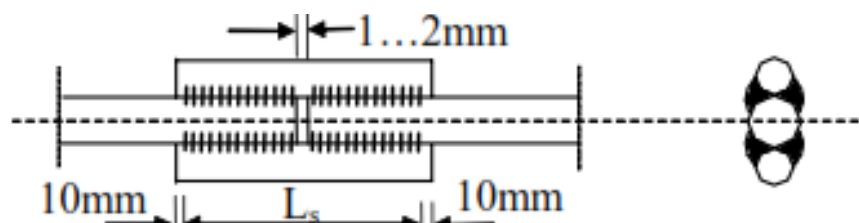
b) layered fabric (longitudinal section)

Diametrul barelor (mm)	Lungimi de suprapunere
$\phi \leq 6$	$\geq 150$ mm; cel puțin un ochi de plasă în intervalul de înnădire fig. 5.18a.
$6 < \phi \leq 8,5$	$\geq 250$ mm; cel puțin două ochiuri de plasă în intervalul de înnădire fig. 5.18b.
$8,5 < \phi \leq 12$	$\geq 350$ mm; cel puțin două ochiuri de plasă în intervalul de înnădire fig. 5.18b.

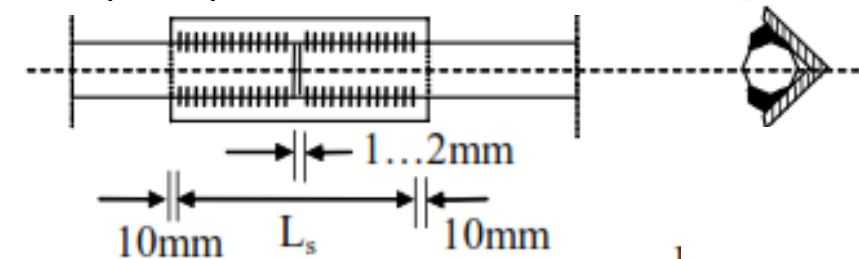
## Welding



welding by overlapping



splice piece

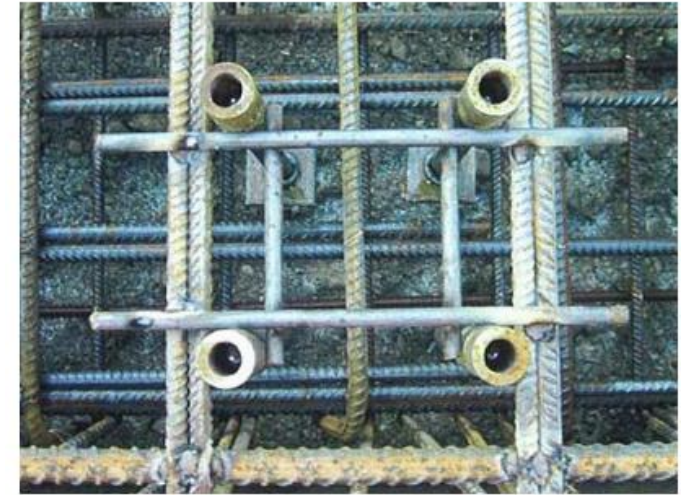
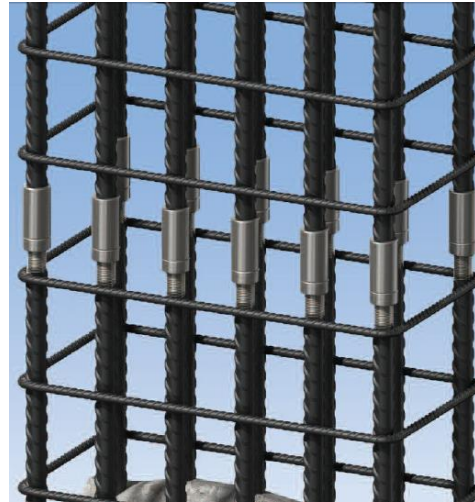


welding with angle profile



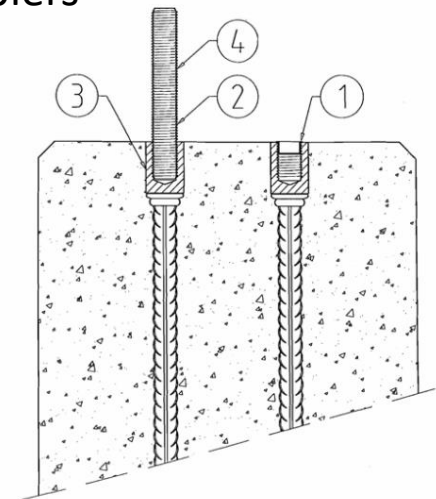
*Welding details will be specified in the design project, together with specific conditions, as well as the permissible deviations.*

## Mechanical couplers

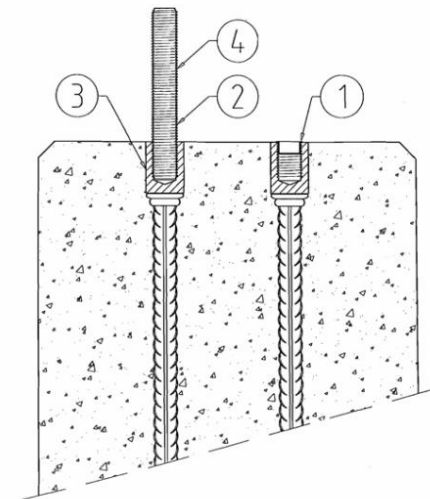
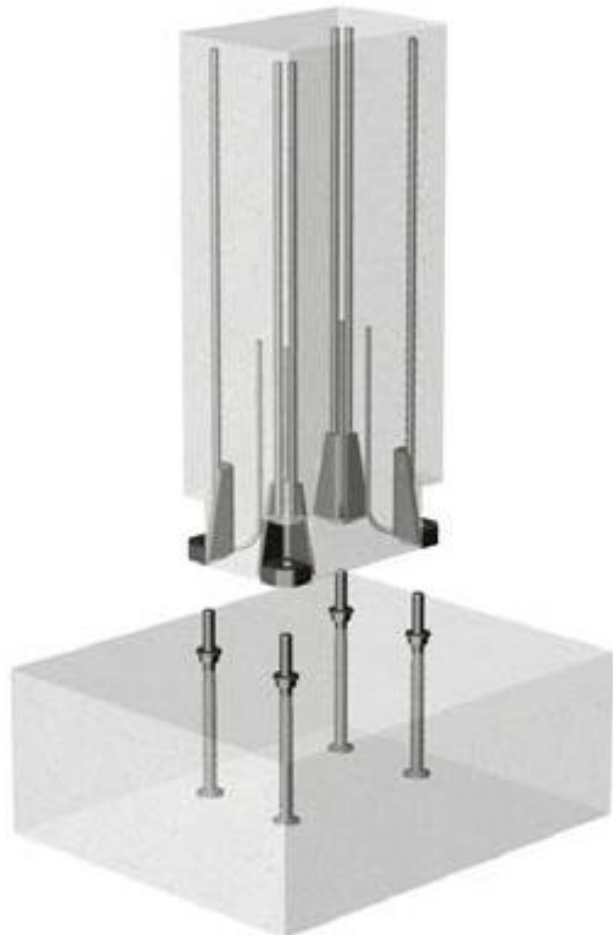


Standard and position couplers

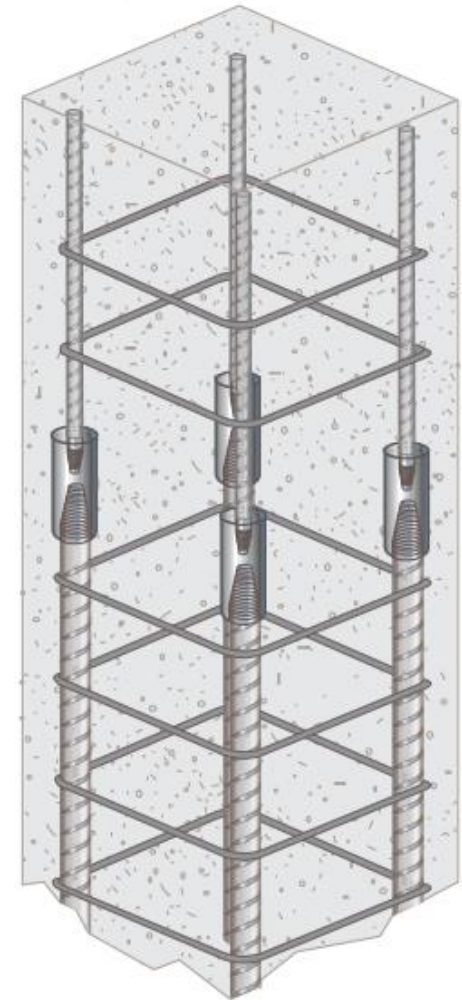
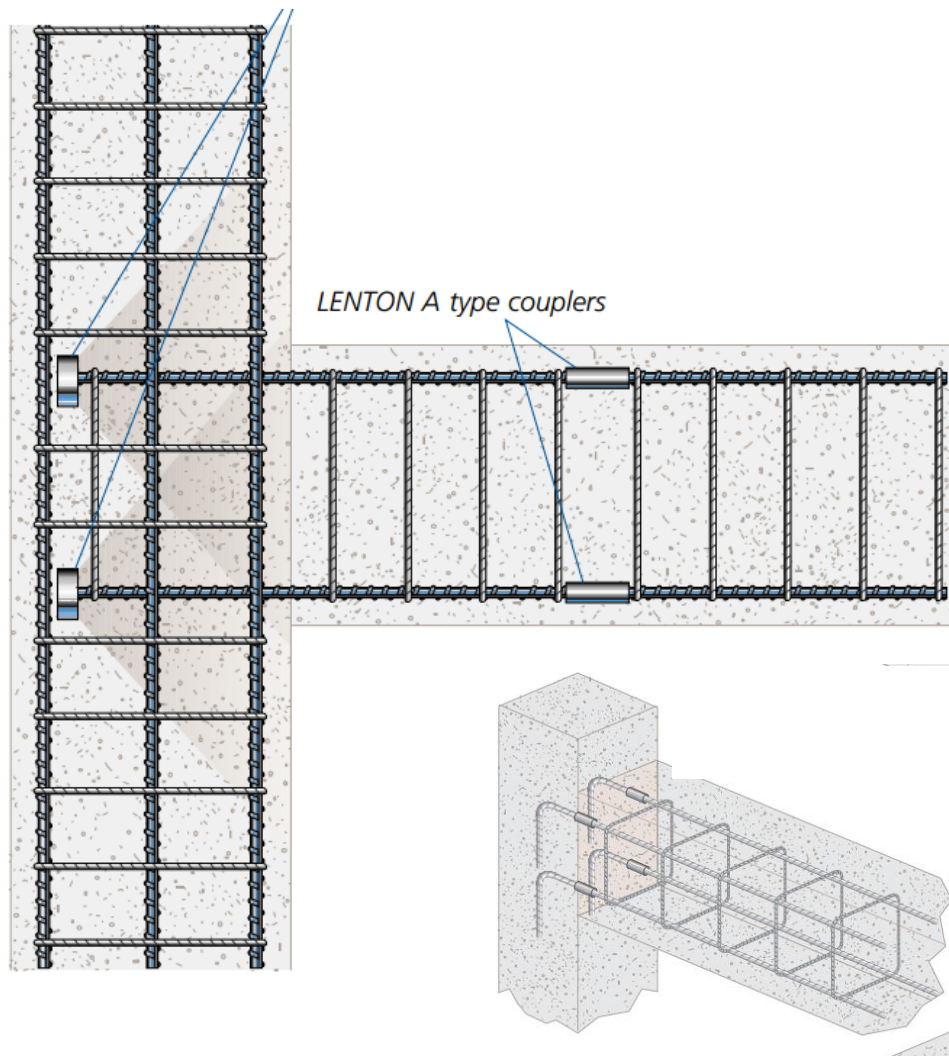
Foundations →



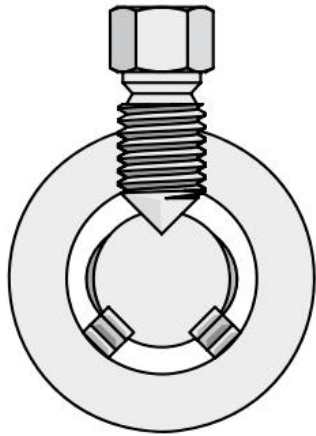
## Mechanical couplers



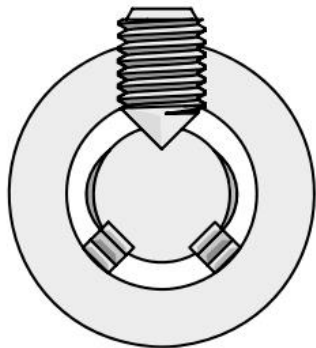
## Mechanical couplers



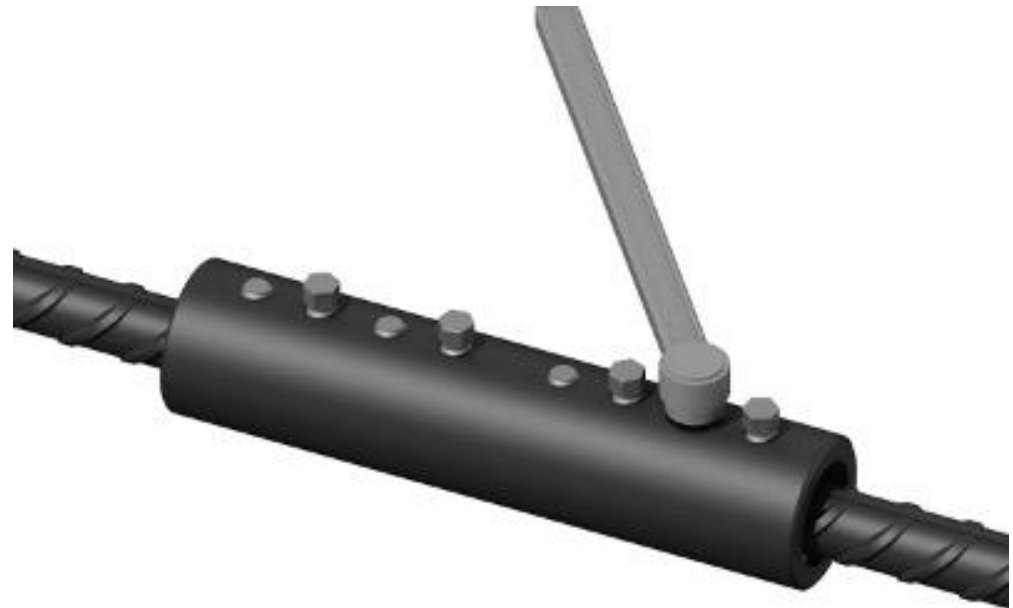
## Mechanical couplers



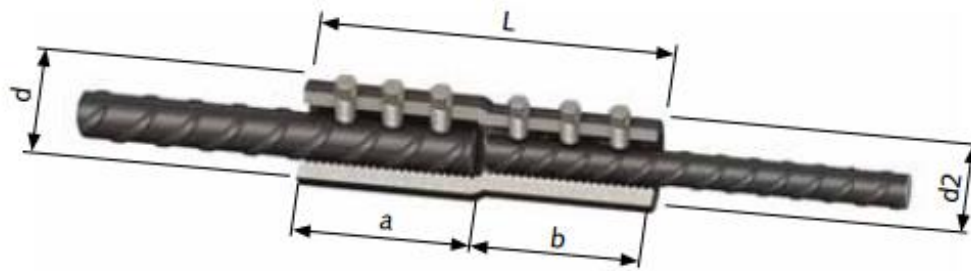
Coupler with screwed-in shear-off screw



Coupler with sheared-off screw head

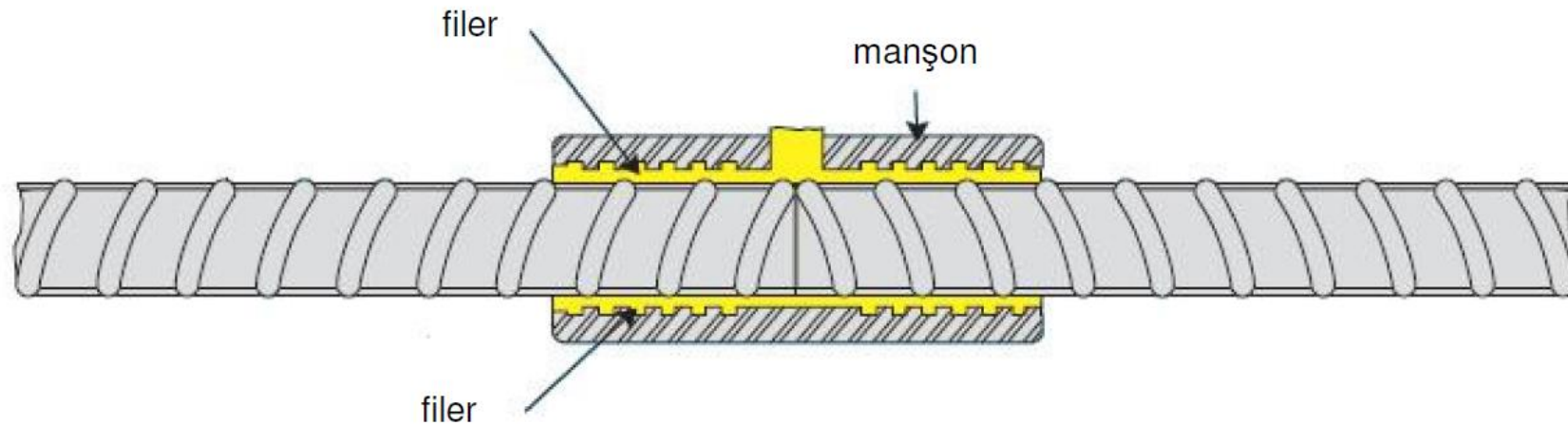


## Mechanical couplers





## Mechanical couplers



## 4.1 REINFORCEMENT ANCHORAGE

# 4.2 WORKING STAGES OF RC ELEMENTS

## 4.3 DURABILITY OF RC

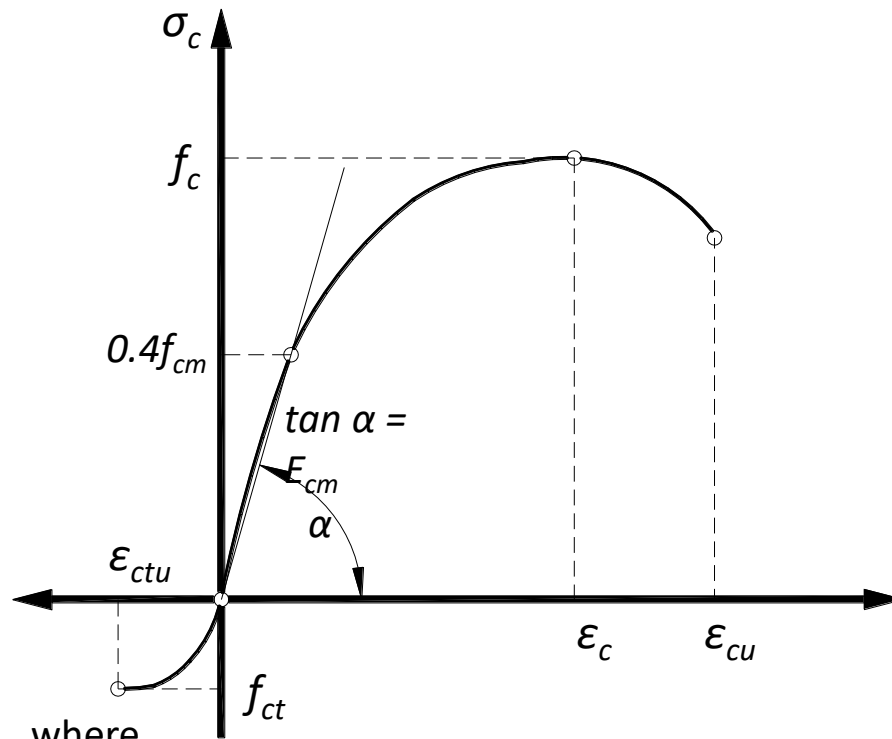
## Working stages / Stadiile de lucru

The behaviour of RC elements depends on the value of internal forces induced by loads.

In time, intensity of internal forces increasing, that leads to changes in stress distributions.

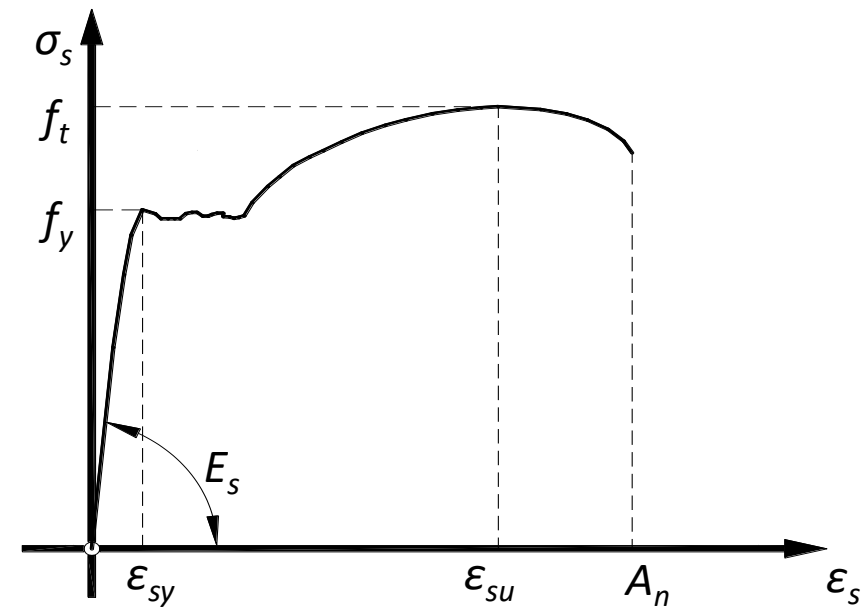
## Working stages / Stadiile de lucru

Concrete and steel has different characteristics, emphasized by the  $\sigma - \varepsilon$  diagrams.



where

- $f_c$  – compressive strength of concrete
- $f_{ct}$  – tensile strength of concrete
- $\varepsilon_{cu}$  – ultimate compressive strain of concrete
- $\varepsilon_{ctu}$  – ultimate tensile strain of concrete
- $E_{cm}$  – secant modulus of elasticity



where

- $f_y$  – yielding limit
- $f_t$  – tensile strength of steel
- $\varepsilon_{su}$  – ultimate tensile strain
- $\varepsilon_{sy}$  – strain at yielding
- $E_s$  – Young's modulus of steel

## Working stages / Stadiile de lucru

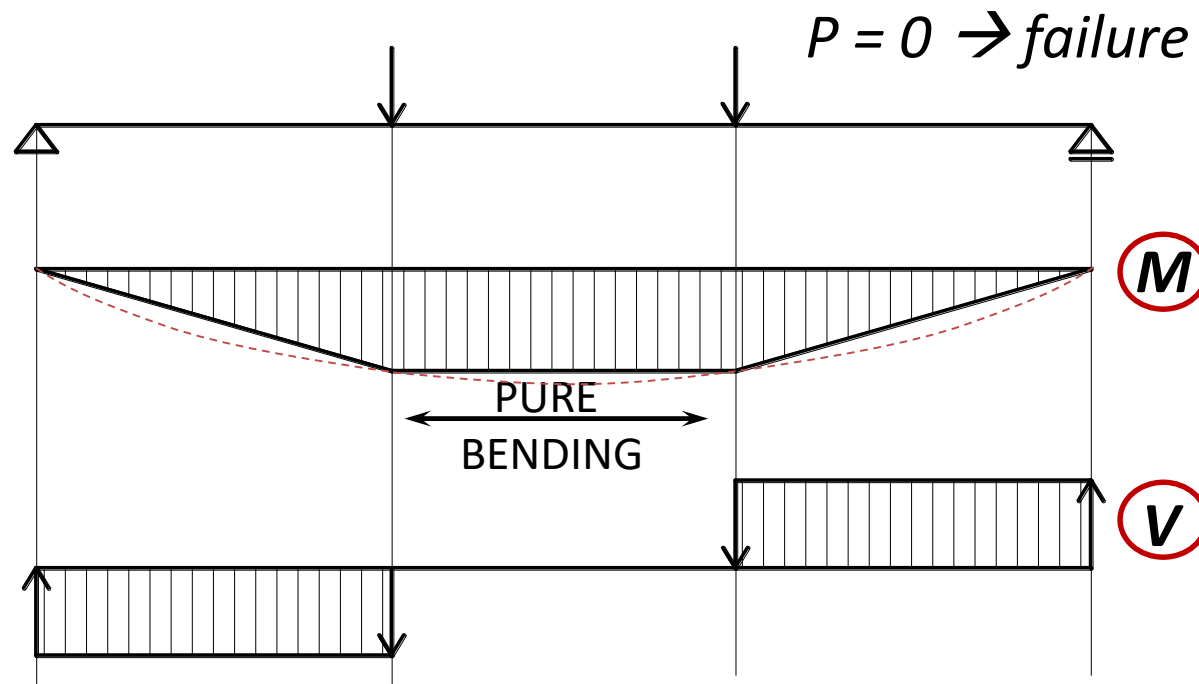
During the life of the element there are the following stages:

**I. Elastic**

**II. Elasto-plastic (service)**

**III. Plastic stage (failure)**

To discuss these stages → consider a simply supported beam



## Working stages / Stadiile de lucru

**STAGE I.**

- Low value of loads
- Concrete is uncracked → entire cross section is active
- Bending stiffness is maximum (EI)
- Mainly elastic behavior

**Limit of Stage I.**

$$\varepsilon_{ct} = \varepsilon_{ctu}$$



$$\sigma_{ct} = f_{ct}$$

- plastic deformations are produced in the tensioned concrete at the limit of the stage

- at the limit of the stage, for a very small increasing of loads, tensioned concrete will crack;  $M_{cr}$  = cracking bending moment.

## Working stages / Stadiile de lucru

**STAGE I.**

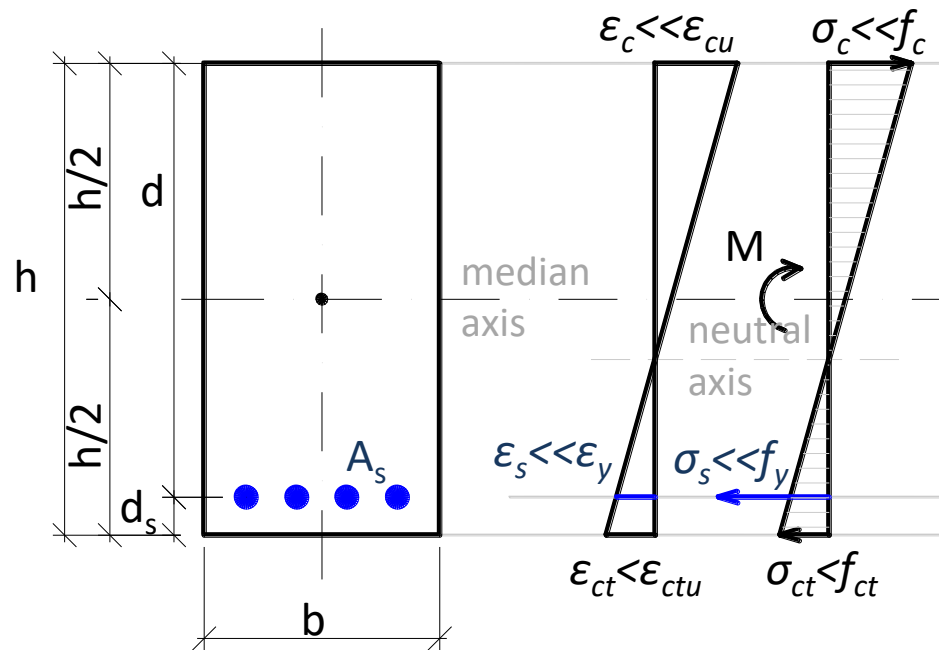
→ Design in stage I is generally used for hydro-technical structures.

Design in stage I is not economical because the stress in reinforcement is very small

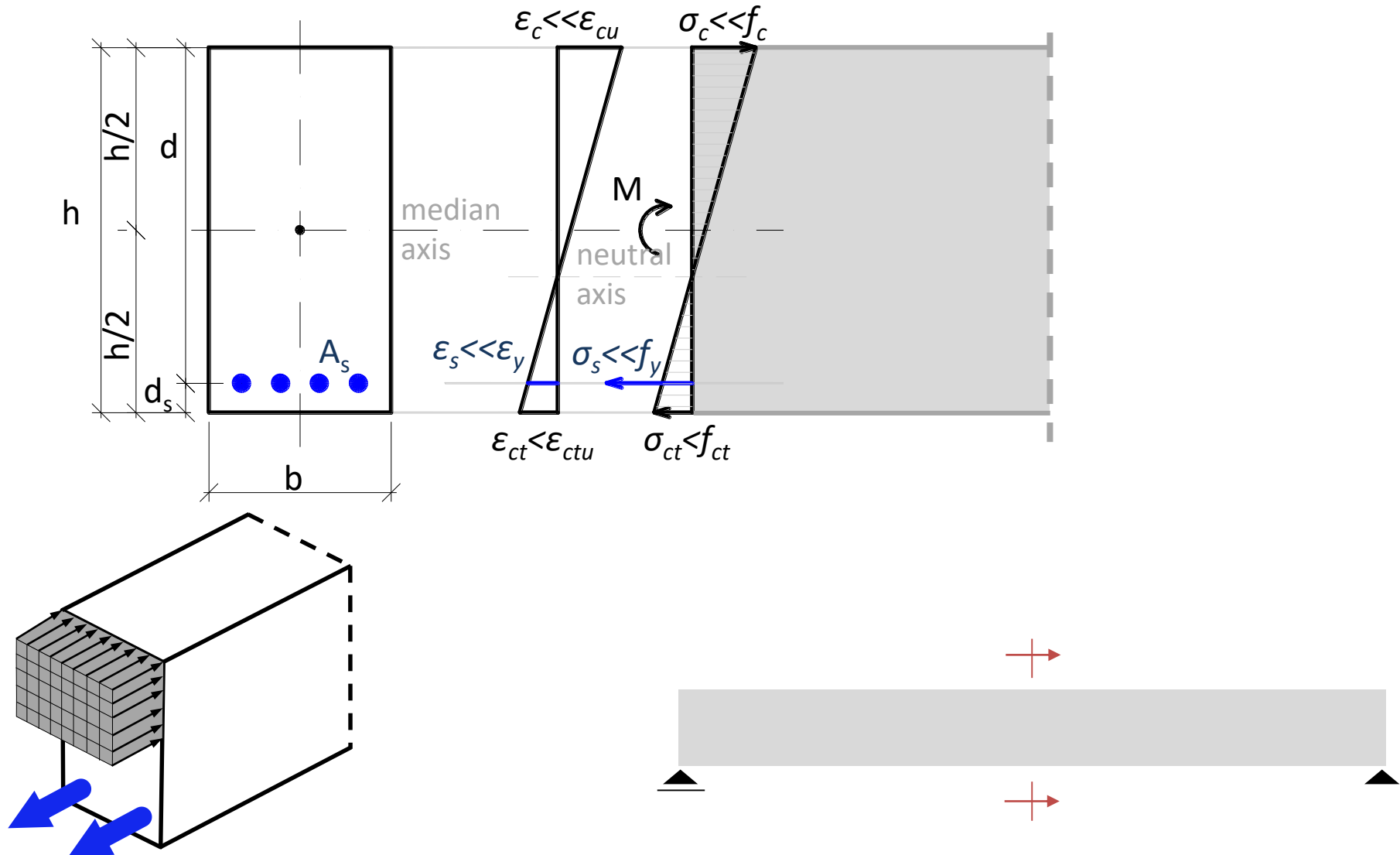
→ Reinforcement is not used to at its capacity.

$$\sigma_s = \varepsilon_s \cdot E_s \approx \varepsilon_{tu} \cdot E_s = \frac{0.10 \dots 0.15}{1000} \cdot 210000 = 21 \dots 30 \text{ N/mm}^2 \ll f_y = 210 \dots 500 \text{ N/mm}^2$$

$\swarrow$   
 $\approx 0.1 \dots 0.15\text{‰}$

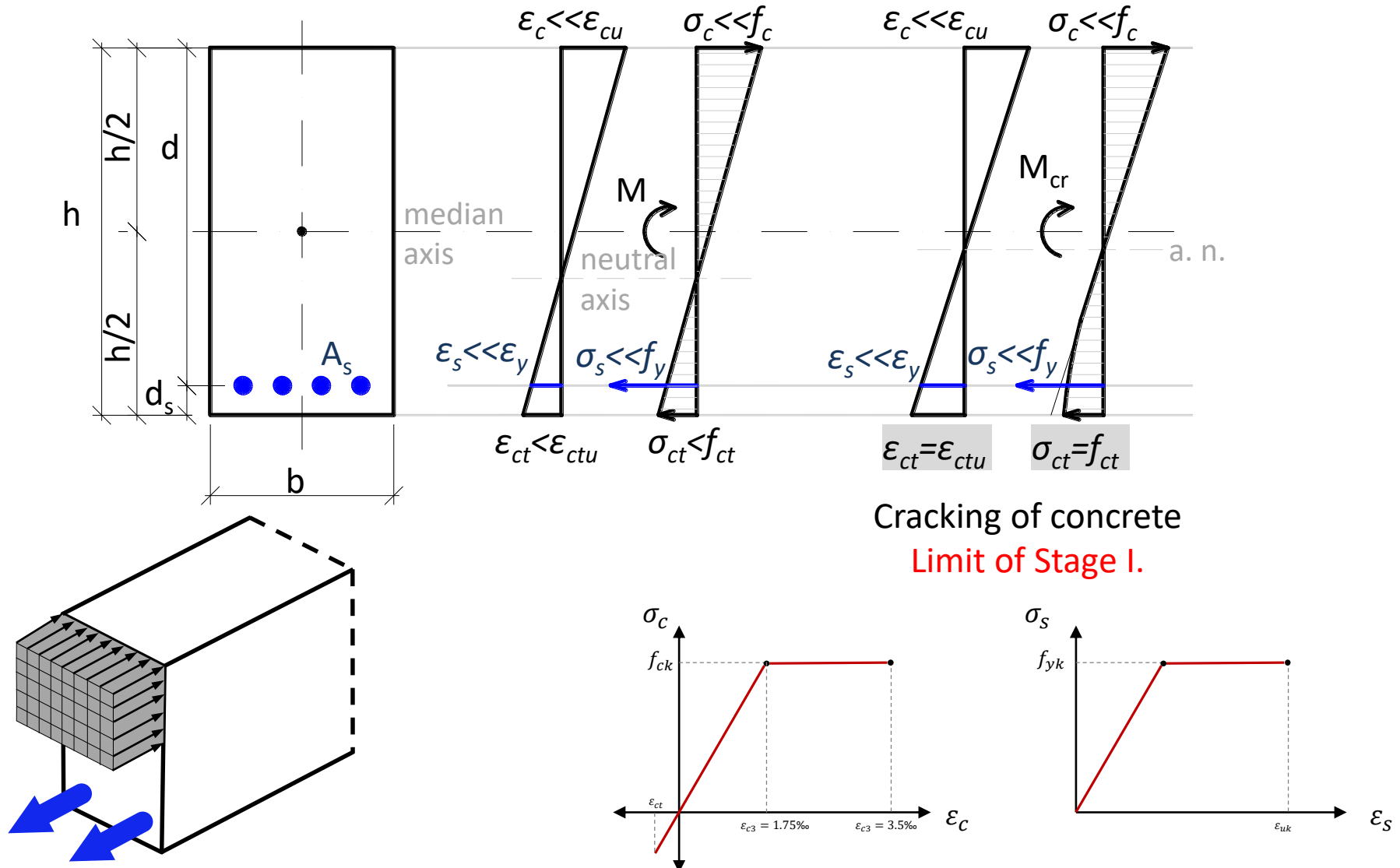


## Working stages / Stadiile de lucru

**STAGE I.**

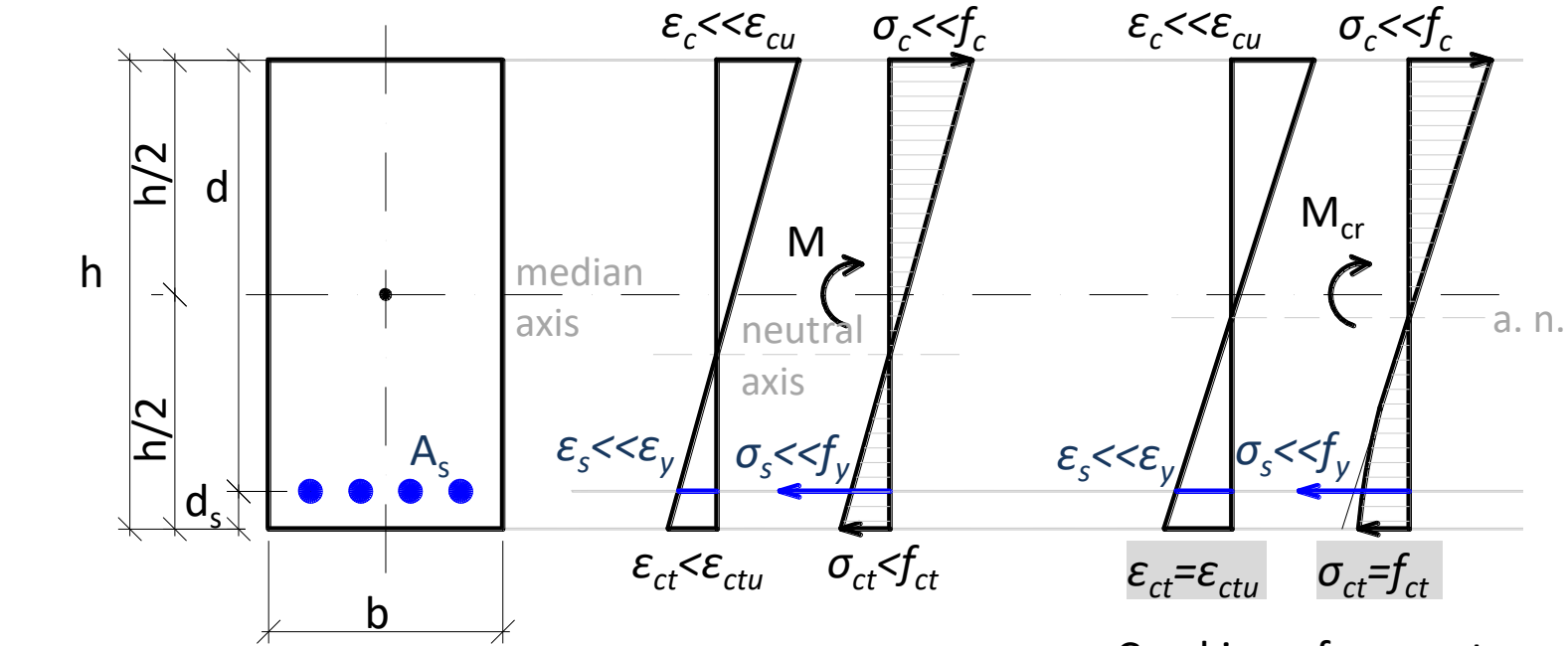


## Working stages / Stadiile de lucru

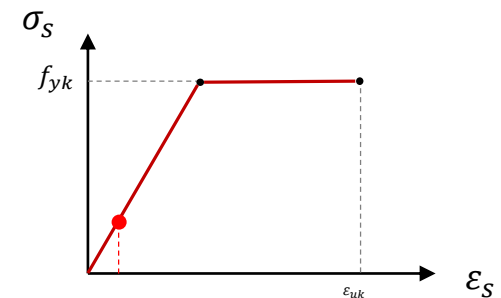
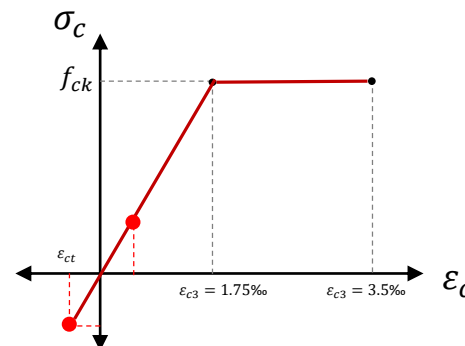
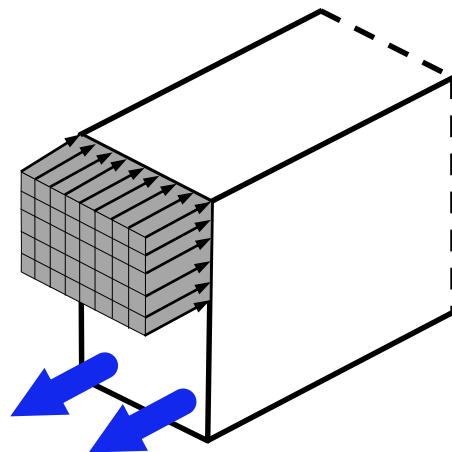
**STAGE I.**

Working stages / Stadiile de lucru

**STAGE I.**



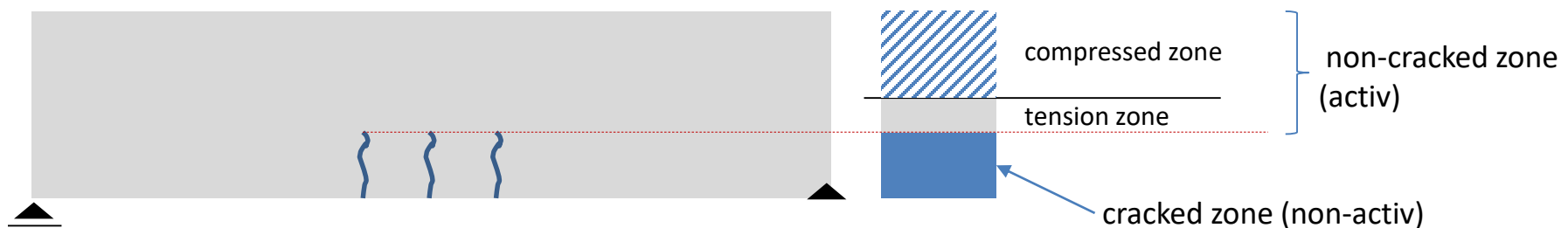
Cracking of concrete  
Limit of Stage I.



## Working stages / Stadiile de lucru

### STAGE II. – service stage

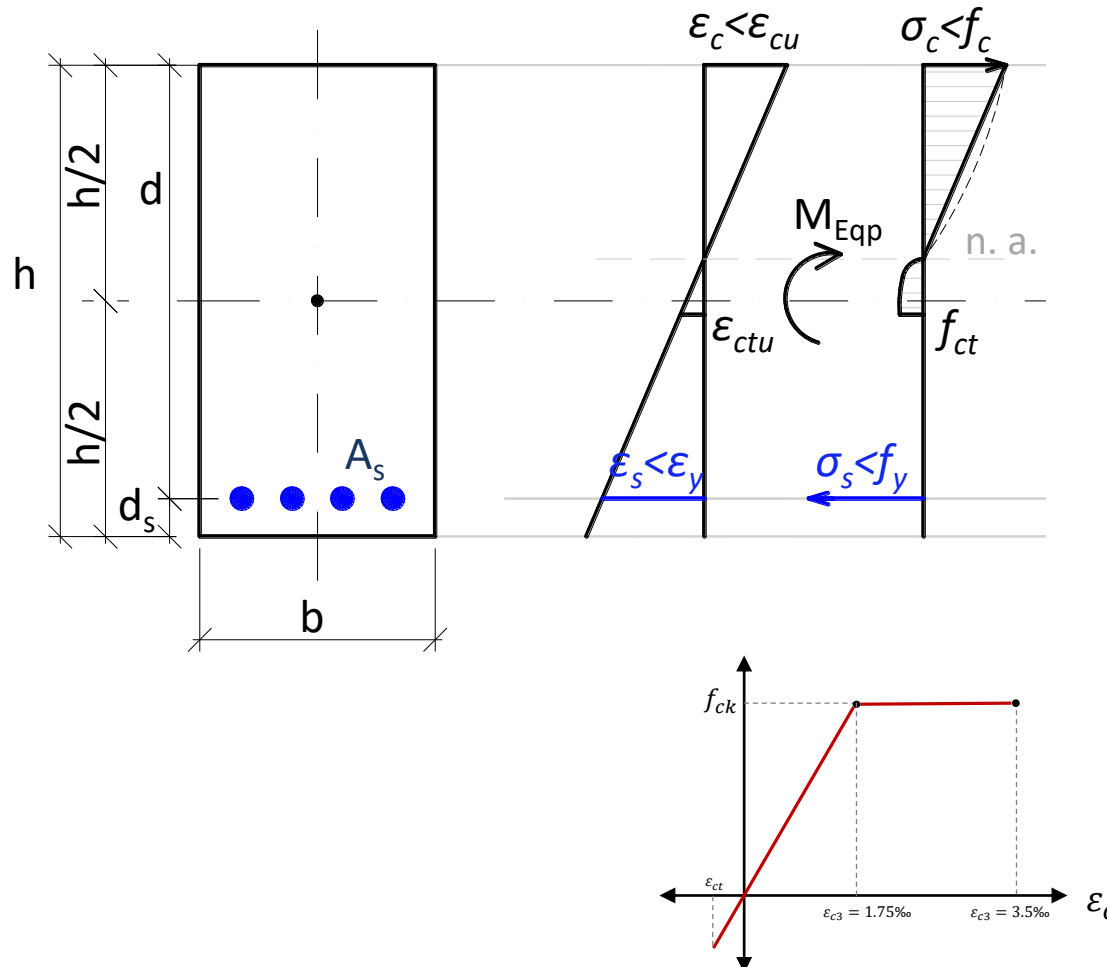
- under service loads, tension zone of the element is cracked
- concrete in tension is neglected
- active section consists of compressed concrete and tension reinforcement
- bending stiffness ( $EI$ ) of the section decreases as a result of cracking
- generally, elastic behaviour, characterized by:
  - in compressed concrete:  $\sigma_c \approx 0,5 f_c$
  - in tensioned reinforcement:  $\sigma_s \approx 0,7 \dots 0.8 f_y$



## Working stages / Stadiile de lucru

**STAGE II. – service stage**

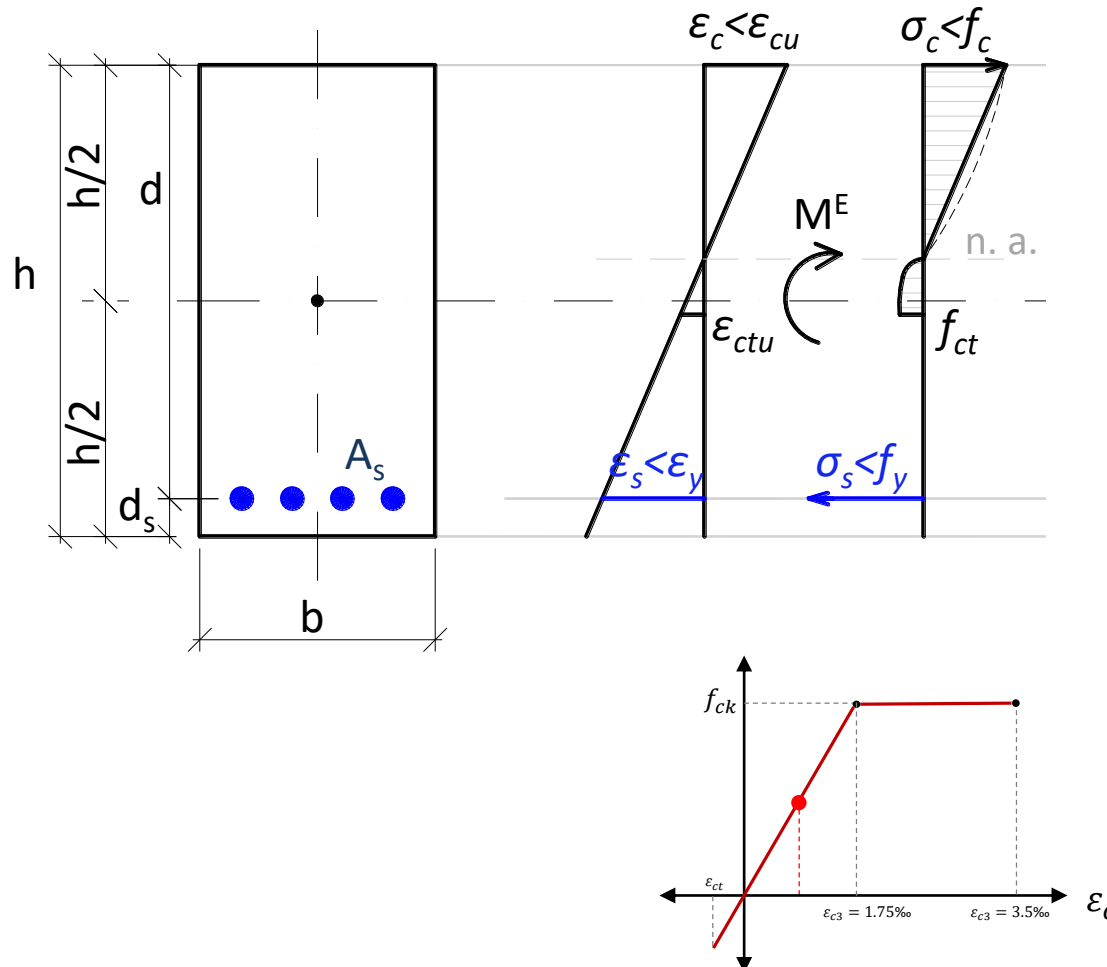
→ Is the basis of design for SLS and fatigue



## Working stages / Stadiile de lucru

**STAGE II. – service stage**

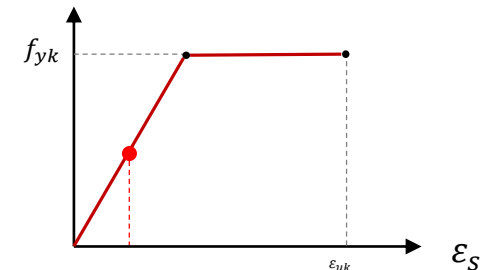
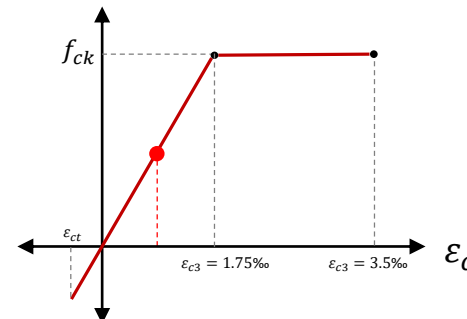
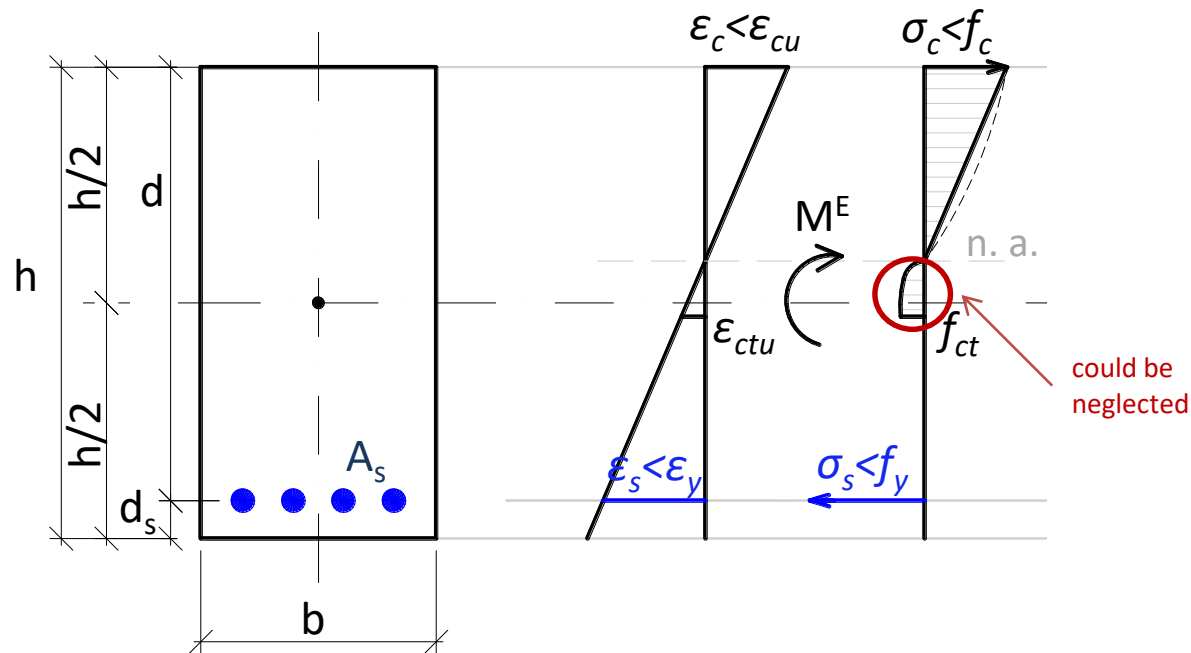
→ Is the basis of design for SLS and fatigue



## Working stages / Stadiile de lucru

**STAGE II. – service stage**

→ Is the basis of design for SLS and fatigue

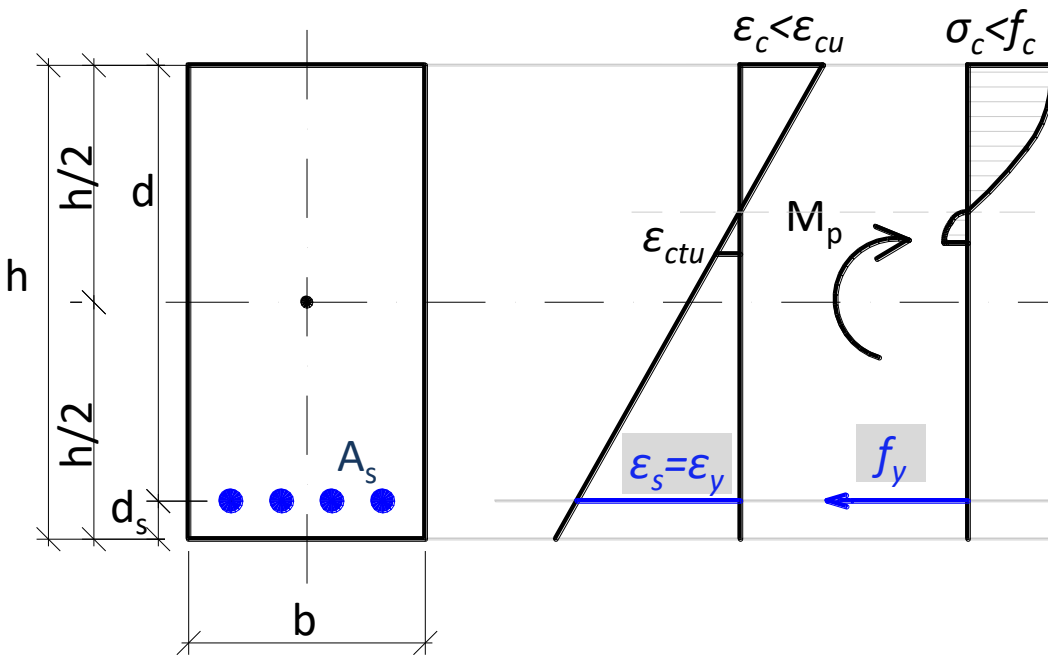


## Working stages / Stadiile de lucru

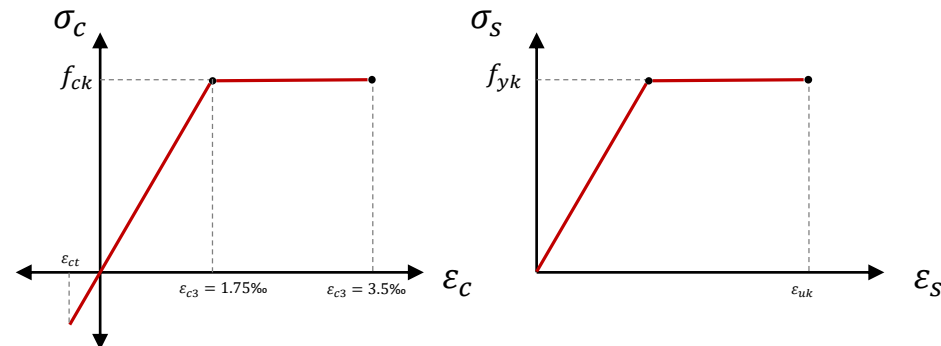
**STAGE III. – Failure stage**

- Increasing of loads leads to further increase of strains and stresses
- Reinforcement starts to yield in case of usual reinforcement percentages ( $p = 0,3...2,5\%$ )
- Under constant loads there is a progressive rotation of the section induced by reinforcement yielding. This situation is defined as plastic hinge involving the curved diagram in compressed concrete  $\rightarrow$  corresponding the bending moment  $M_p = A_s f_y z \approx 0,9 A_s f_y d$  ( $p = \text{plastic}$ )
- stiffness decreasing, deformations increasing, neutral axis rising toward the maximum point  $\rightarrow$  Minimum bending stiffness & very high deflection
- further increasing of loads leads finally to crushing of compressed concrete  $\rightarrow$  corresponding to  $M_R$  (failure or resisting moment).
- the failure is ductile, because of the large deformations before the collapse.

## Working stages / Stadiile de lucru

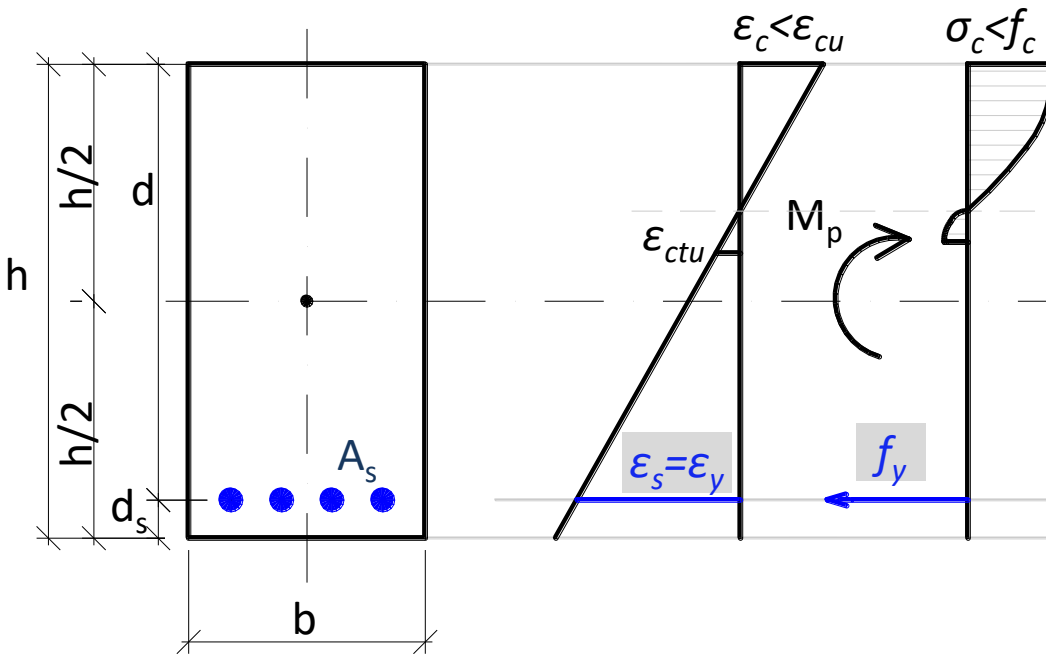
**STAGE III. – Failure stage**

Reinforcement yielding

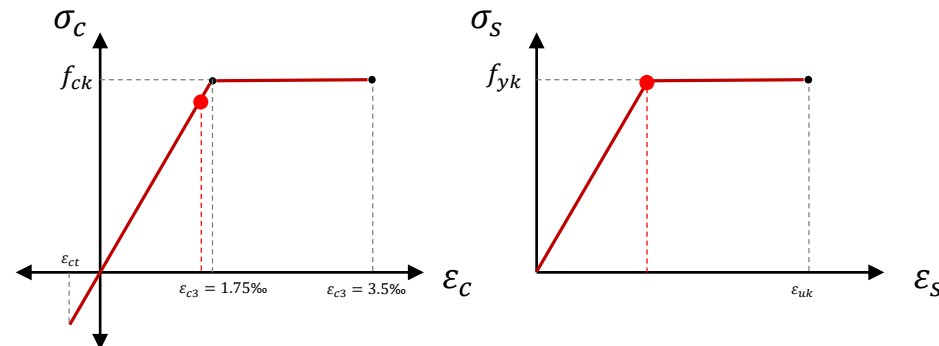




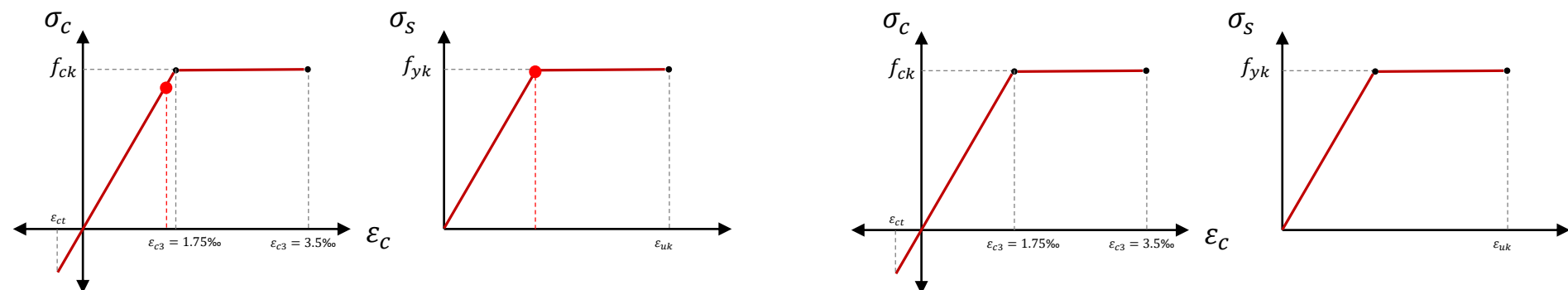
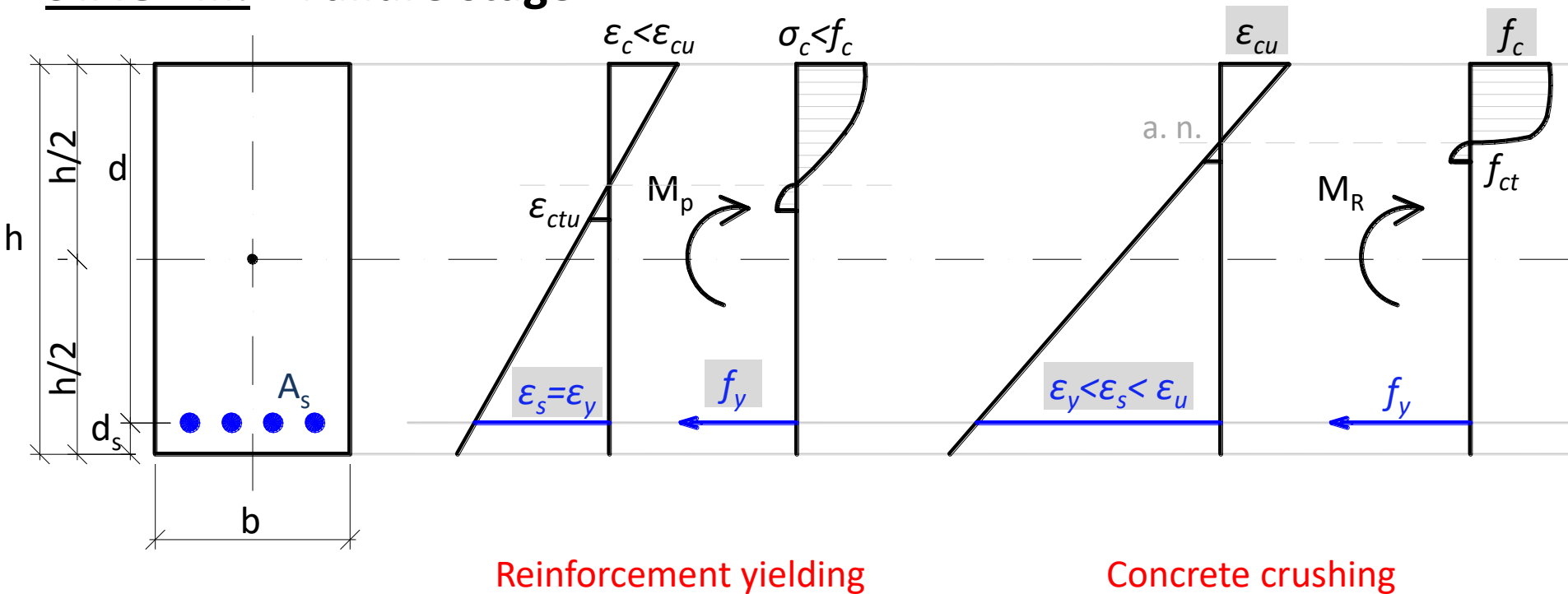
## Working stages / Stadiile de lucru

**STAGE III. – Failure stage**

Reinforcement yielding

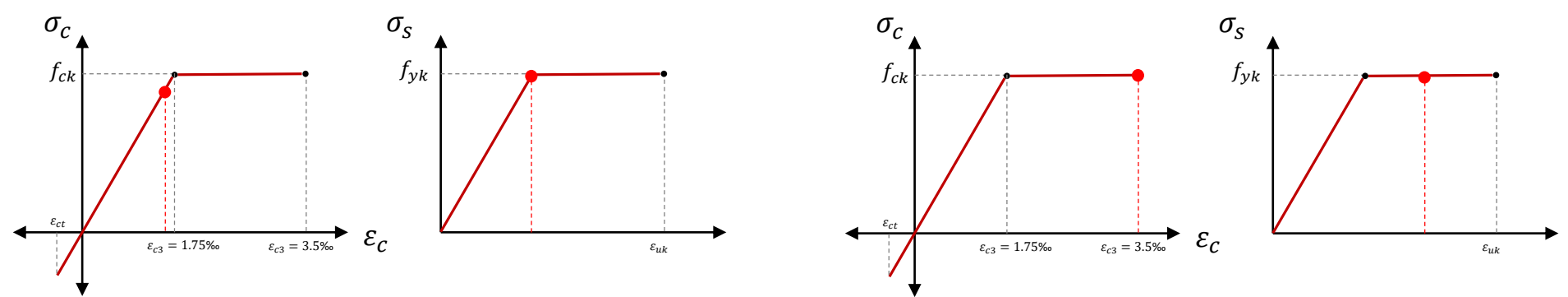
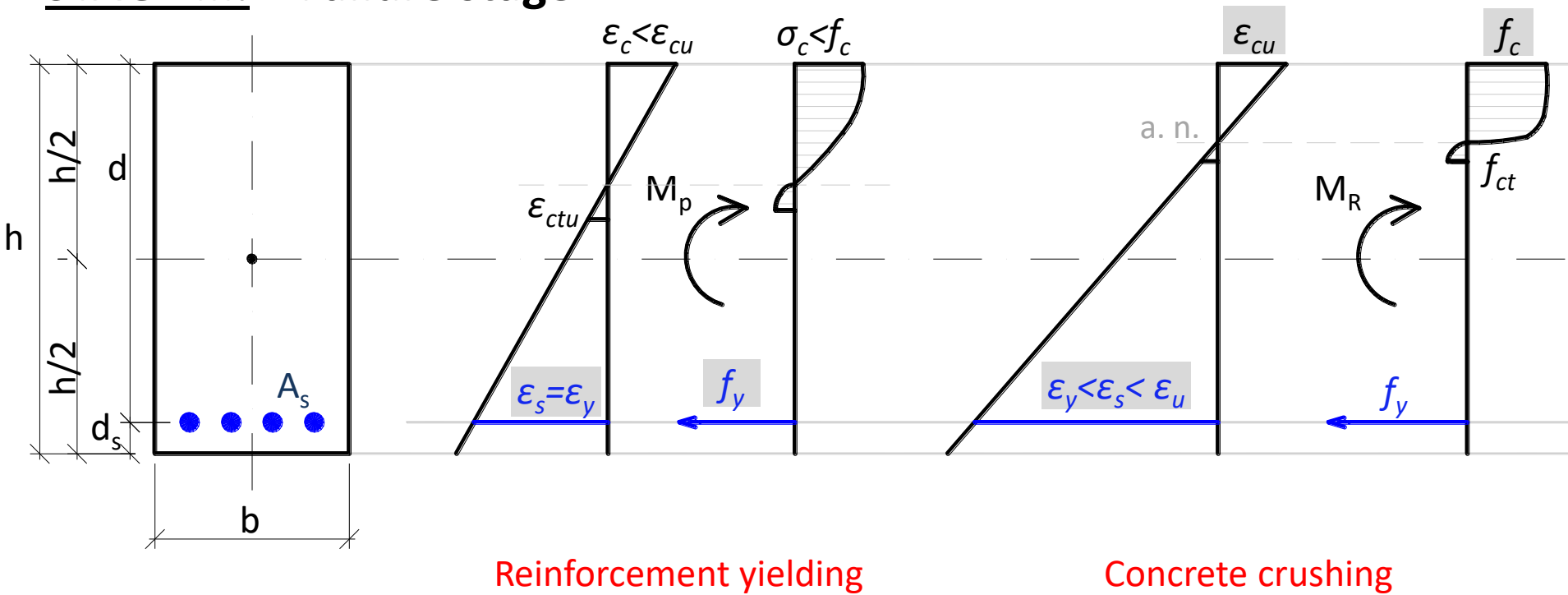


## Working stages / Stadiile de lucru

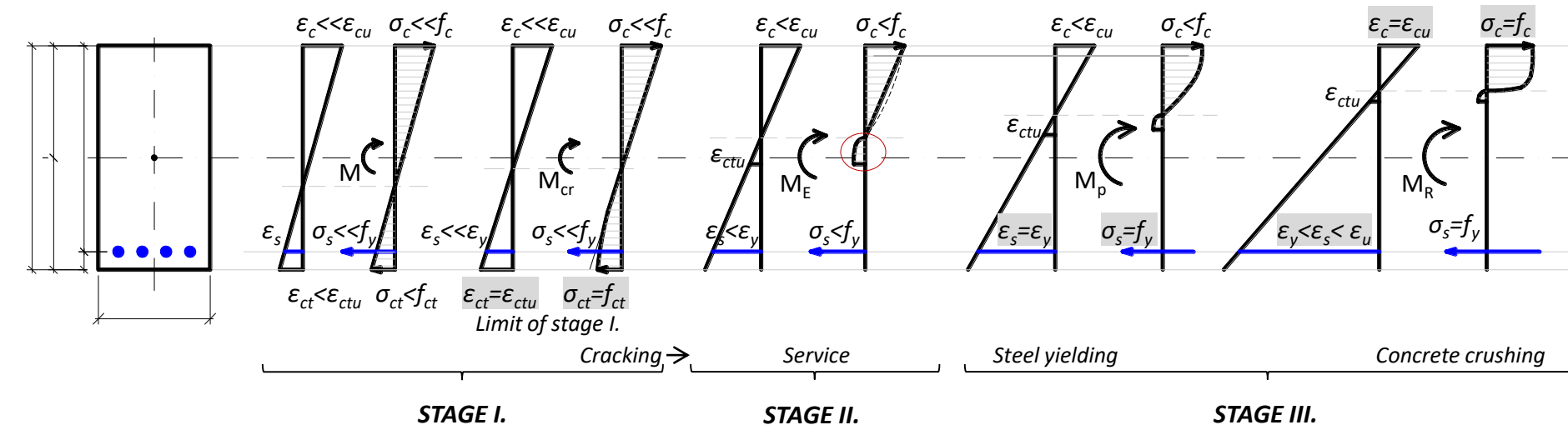
**STAGE III. – Failure stage**

Working stages / Stadiile de lucru

**STAGE III. – Failure stage**



## Working stages / Stadiile de lucru



- a)
- entire section is active
  - elastic deformations
  - n.a. is under the element axis
  - element stiffness is maximum
  - instable stage
- b)
- plasticization of tensioned concrete
  - $M_{cr}$  – cracking moment

- reducing the stiffness
- active zones: compressed concrete and tensioned rebar
- n.a. rising above the element axis

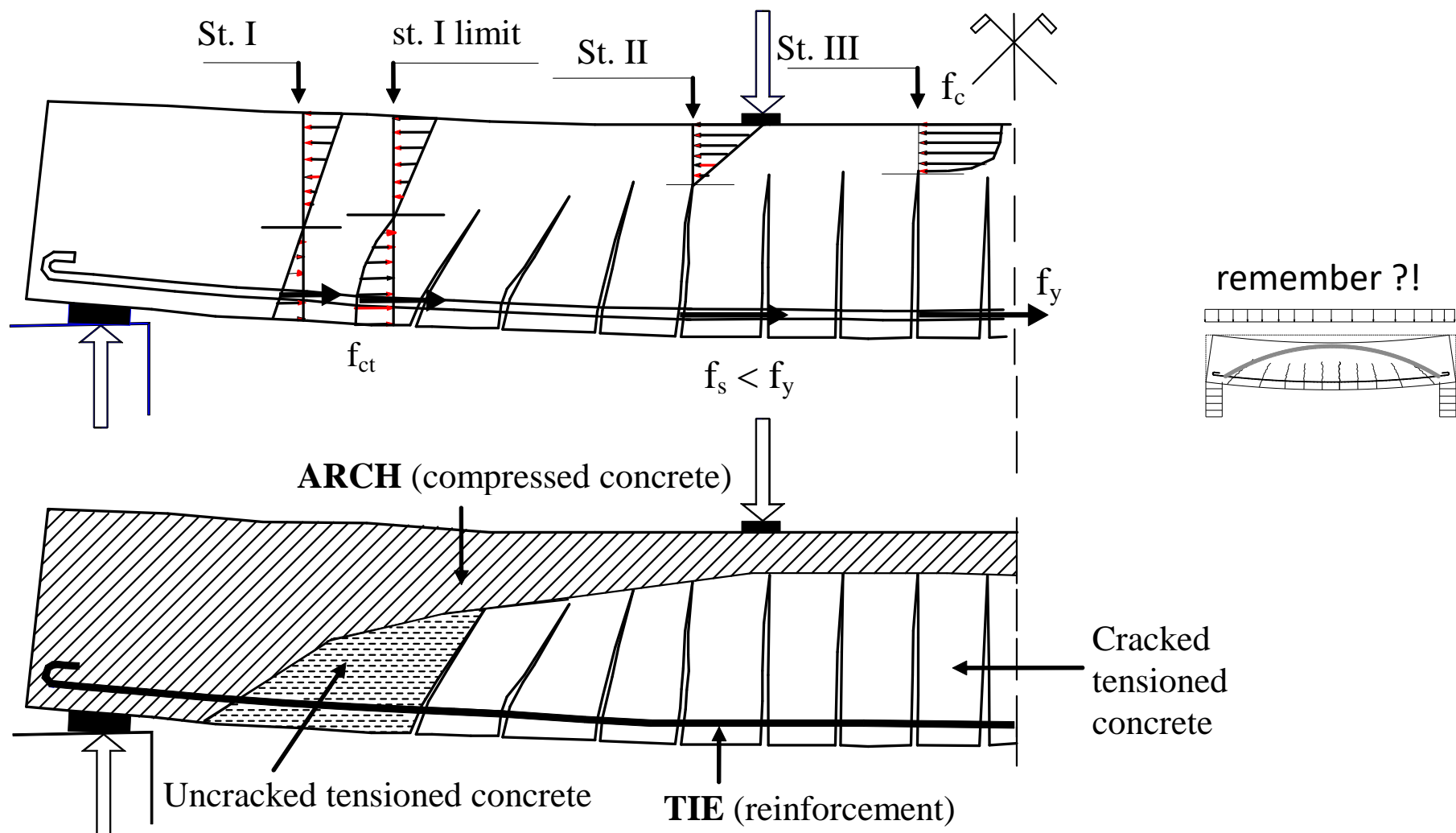
$$\sigma_c \cong 0.5f_c$$

$$\sigma_s \cong (0.7 \div 0.8)f_y$$

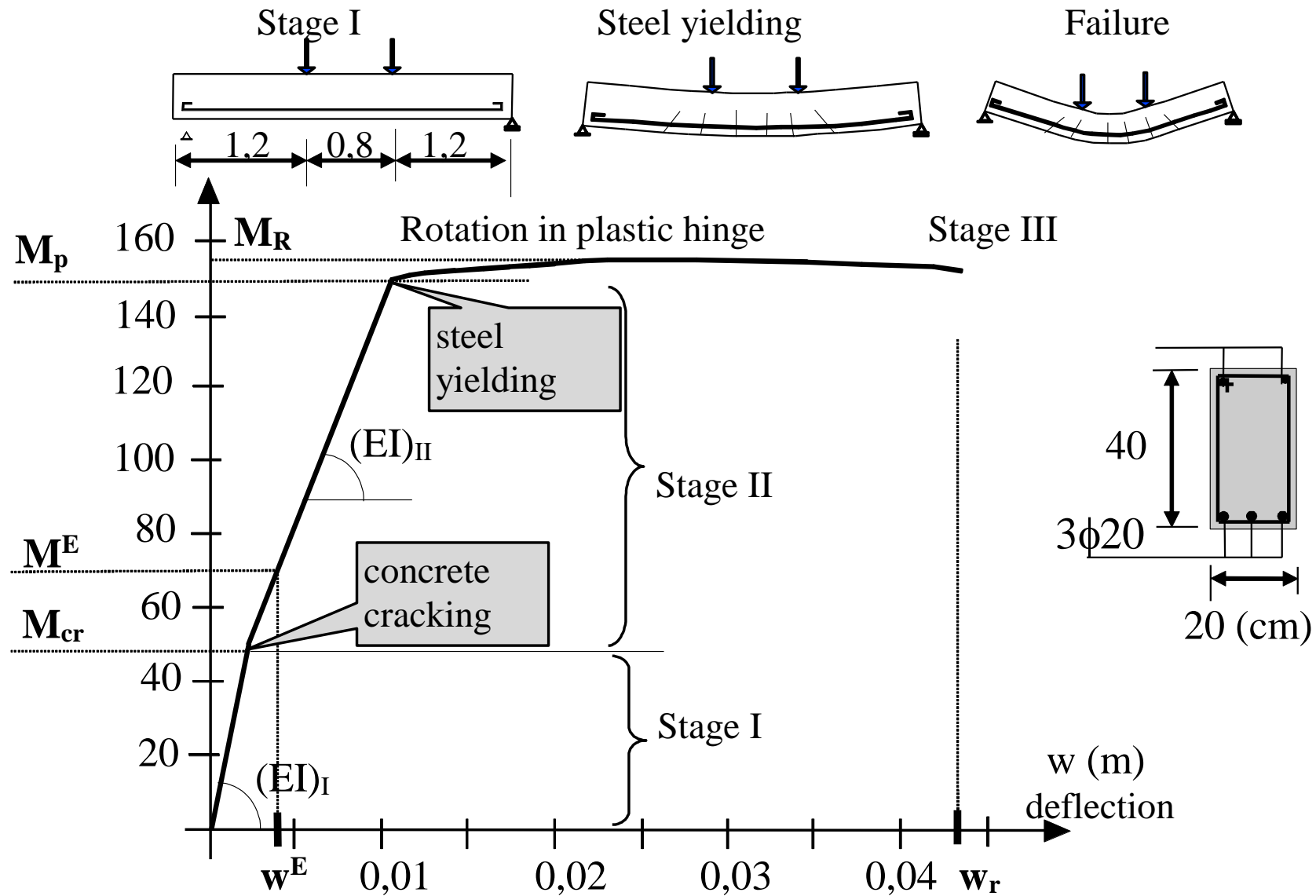
- a)
- increasing of deformations
  - yielding of reinforcement
  - plastic deformation of concrete
  - forming of plastic hinges
  - $M_p \approx 0.9A_s f_y d$
- b)
- n.a. in the maximum position
  - stiffness of the section is minimum
  - very large deformations
  - failure by crushing of compressed concrete
  - ductile behaviour

## Working stages / Stadiile de lucru

- Along the element could be find all the working stages.
- The element works as a concrete arch with a steel tie



## Working stages / Stadiile de lucru



## FINAL REMARKS

- Failure of RC elements having **usual reinforcement percentage** between **0.4 ÷ 2.0 (2.5)%** begins with yielding of reinforcement and finishing by crushing of compressed concrete.

- Elements with great value of reinforcement percentage = **over-reinforced concrete** → no more yielding of reinforcement, failure is produced by crushing of compressed concrete

Is not advisable to use such case:

- reinforcement is not yield → not economical
- failure is a brittle-one

- Element with low reinforcement percentage = **under-reinforced concrete** → failure is produced by tensile failure of reinforcement, without crushing of compressed concrete → used in massive constructions.

$$\rho\% = A_s/A_c \times 100 \rightarrow \text{reinforcement percentage}$$

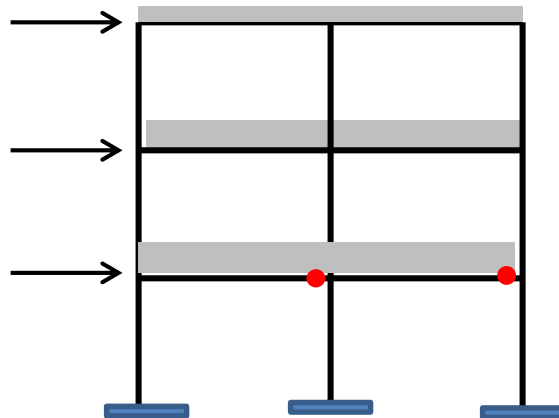
## FINAL REMARKS

### STATICALLY DETERMINATED STRUCTURES

Plastic hinge shows immediate failure



### STATICALLY INDETERMINATE STRUCTURES



Plastic hinge:

- structure still stands
- reduction of the static indeterminacy
- redistribution of efforts to other areas
- **ensure dissipation of the seismic energy**

**BASIC PRINCIPLE OF SEISMIC DESIGN**



## 4.1 REINFORCEMENT ANCHORAGE

## 4.2 WORKING STAGES OF RC ELEMENTS

## **4.3 DURABILITY OF RC**

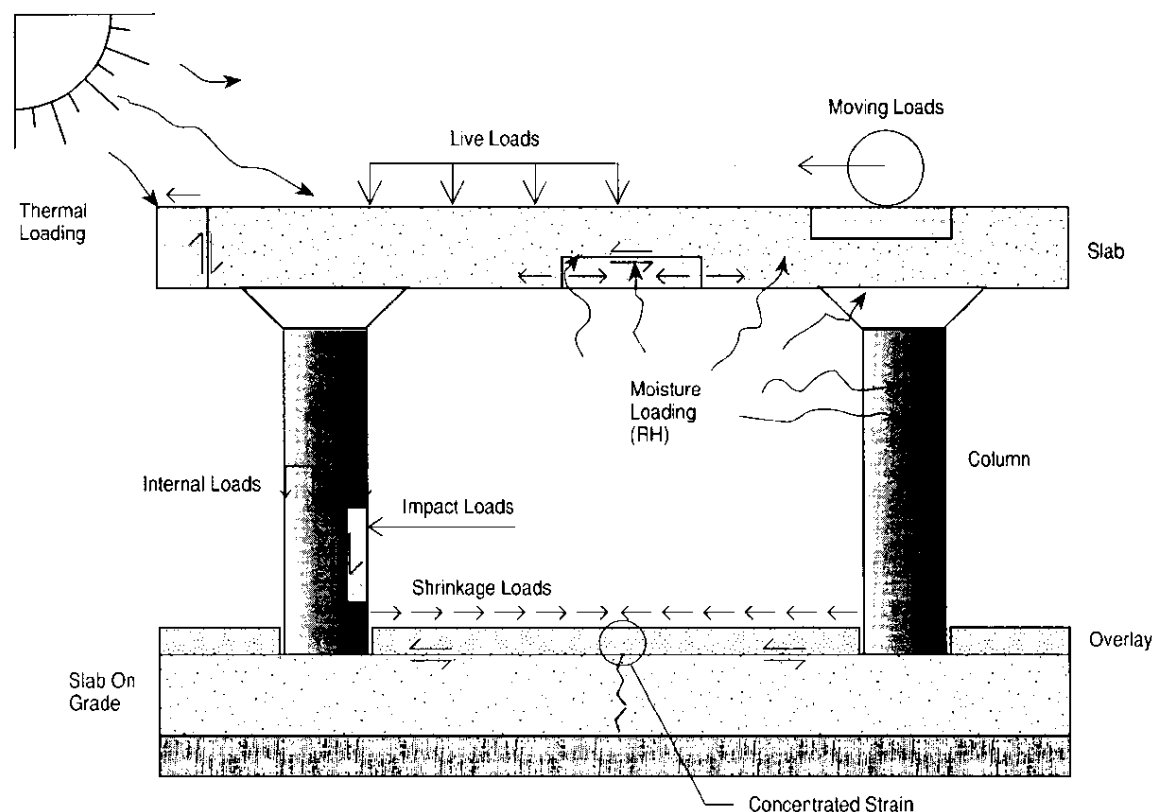
## Durability / Durabilitatea

### Definition

A durable structure shall meet the requirements of serviceability, strength and stability throughout its design working life, without significant loss of utility or excessive unforeseen maintenance.

- Corrosion: carbonation or chlorides
- Freeze-Thaw
- Alkali-silica reactions

Factors affecting structures →



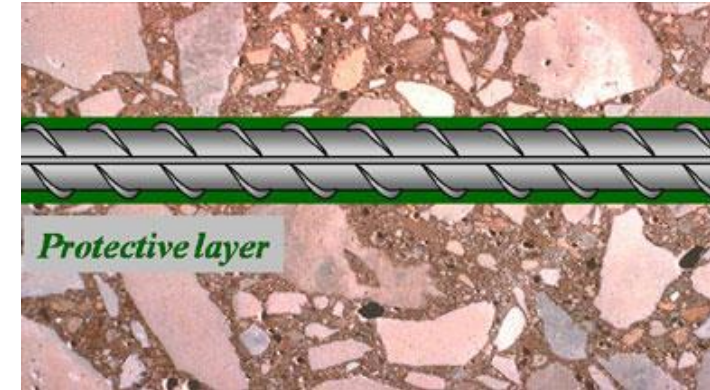
**Durability / Durabilitatea**

Reinforcement corrosion – initiated by chlorides

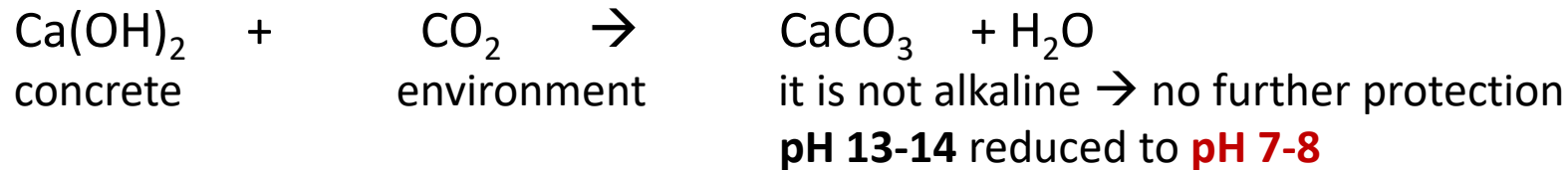


## Durability / Durabilitatea

Reinforcement corrosion – initiated by carbonation



In time →



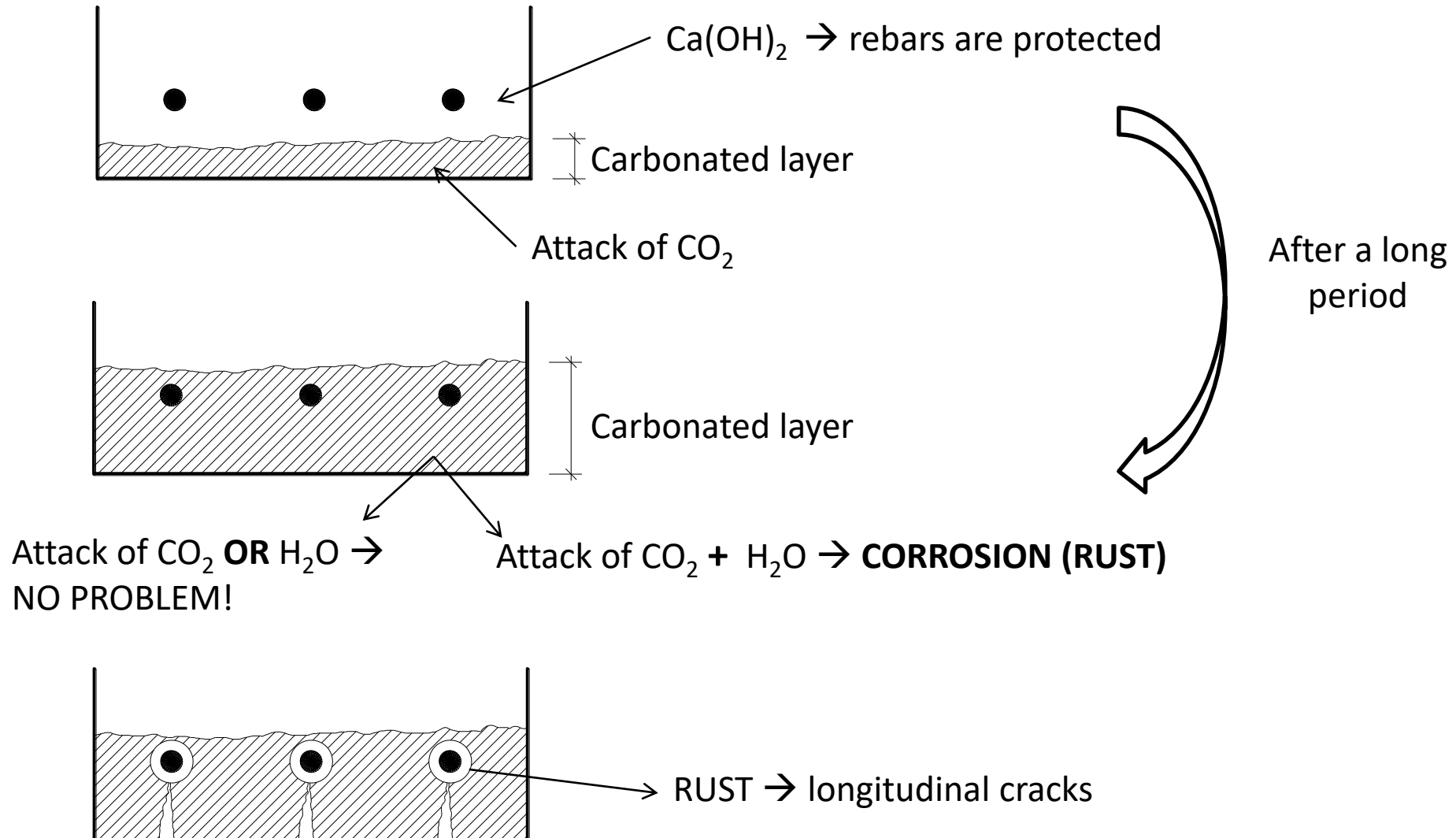
$\text{CO}_2$  → nothing happens!  
 $\text{H}_2\text{O}$  → nothing happens!



After depassivation  $\text{H}_2\text{CO}_3$  attack reinforcement → corrosion (rust)

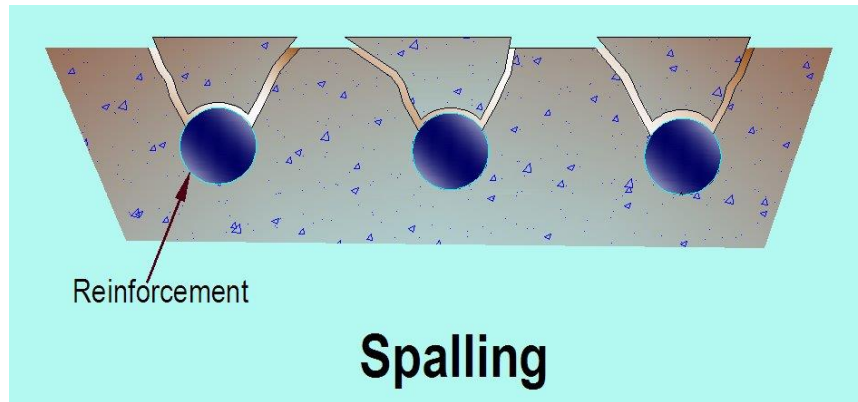
## Durability / Durabilitatea

Reinforcement corrosion – initiated by carbonation



# Durability / Durabilitatea

## Reinforcement corrosion – initiated by carbonation



# Durability / Durabilitatea

## Freeze-Thaw attack



# Durability / Durabilitatea

## Reinforcement corrosion - superposed effects





**Durability / Durabilitatea**

Construction design lifetime (for guidance)

<b>Category</b>	<b>Construction design lifetime (in years)</b>	<b>Type of construction (Examples)</b>
5	=100	Important constructions, monumental buildings
4	50 – 100	Structures for buildings and current constructions
3	15 – 30	Structures for farm buildings or similar
2	10 – 25	Construction parts which could be replaced
1	10	Temporary structures

## Durability / Durabilitatea

Durability of concrete depends on:

- **Exposure conditions:** atmosphere, soil, seawater, salt, mechanical abrasion, storage or contact with chemicals → **exposure class X**
- **Cement type** → in some cases may require special cements resistant to chemicals
- **Concrete quality** → chosen usually from strength condition, but may be required superior classes in certain environmental conditions (density & strength)
- **Thickness of concrete cover** → is calculated according to the exposure class, to protect the reinforcement from penetration of aggressive substances, but also in case of fire
- **Crack width** → if it does not exceed the permissible openings (generally 0.3 mm), are generally not dangerous

***If the factors are favorable, concrete durability could be very high.***

## Durability / Durabilitatea

**O** → no risk of corrosion or attack

**C** → **Carbonation** = corrosion induced by Carbonation

**D** → **Deicing salt** = corrosion induced by chlorides

**S** → **Seawater** = corrosion induced by chlorides

**F** → **Frost** = Freeze/thaw attack

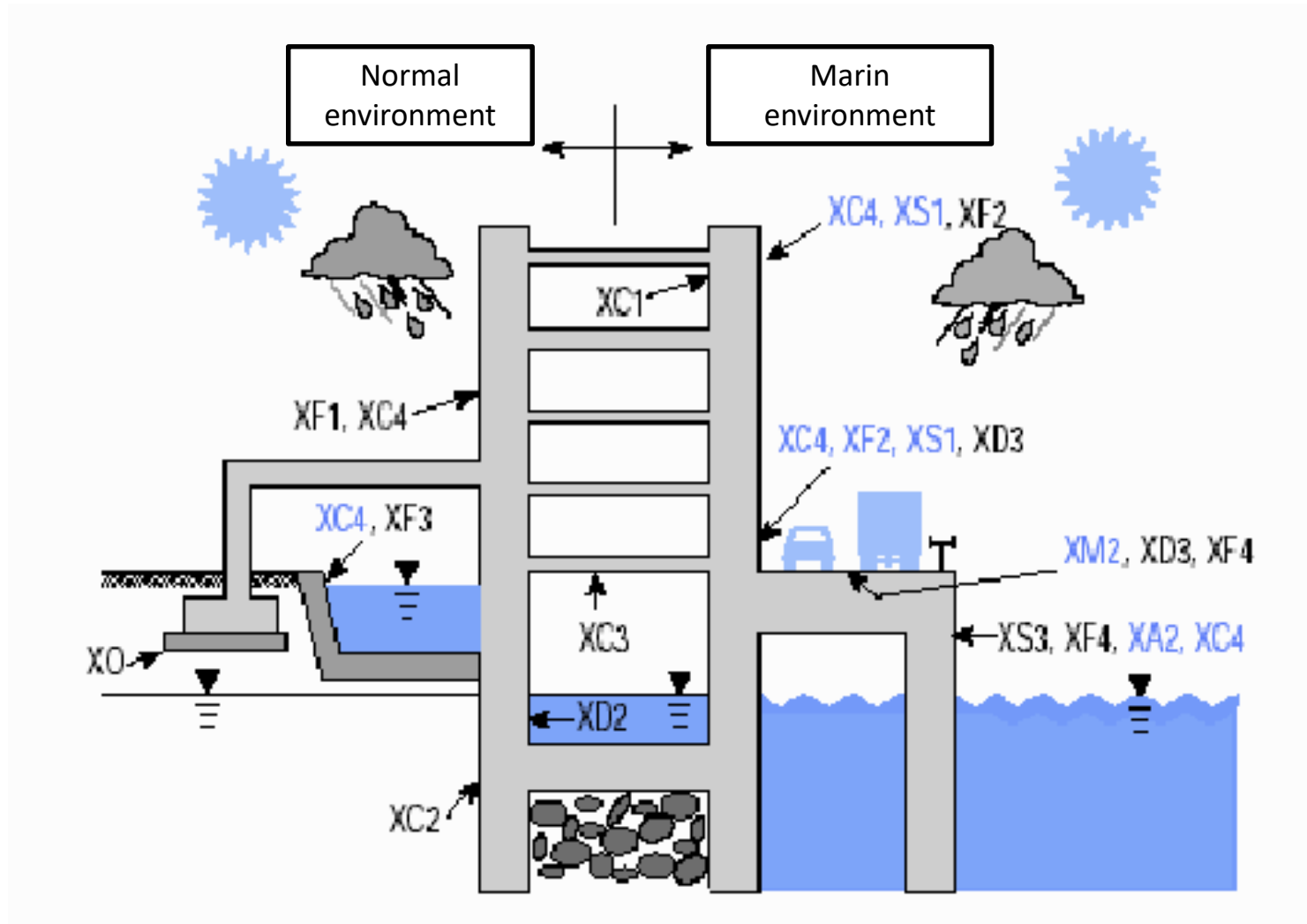
**A** → **Agressive environmet** = chemical attack

**+ M** → **Mechanical abrasion**

Class designation	Description of the environment	Informative examples where exposure classes may occur
<b>1 No risk of corrosion or attack</b>		
X0	For concrete without reinforcement or embedded metal: all exposures except where there is freeze/thaw, abrasion or chemical attack For concrete with reinforcement or embedded metal: very dry	Concrete inside buildings with very low air humidity
<b>2 Corrosion induced by carbonation</b>		
XC1	Dry or permanently wet	Concrete inside buildings with low air humidity Concrete permanently submerged in water
XC2	Wet, rarely dry	Concrete surfaces subject to long-term water contact Many foundations
XC3	Moderate humidity	Concrete inside buildings with moderate or high air humidity External concrete sheltered from rain
XC4	Cyclic wet and dry	Concrete surfaces subject to water contact, not within exposure class XC2
<b>3 Corrosion induced by chlorides</b>		
XD1	Moderate humidity	Concrete surfaces exposed to airborne chlorides
XD2	Wet, rarely dry	Swimming pools Concrete components exposed to industrial waters containing chlorides
XD3	Cyclic wet and dry	Parts of bridges exposed to spray containing chlorides Pavements Car park slabs
<b>4 Corrosion induced by chlorides from sea water</b>		
XS1	Exposed to airborne salt but not in direct contact with sea water	Structures near to or on the coast
XS2	Permanently submerged	Parts of marine structures
XS3	Tidal, splash and spray zones	Parts of marine structures
<b>5. Freeze/Thaw Attack</b>		
XF1	Moderate water saturation, without de-icing agent	Vertical concrete surfaces exposed to rain and freezing
XF2	Moderate water saturation, with de-icing agent	Vertical concrete surfaces of road structures exposed to freezing and airborne de-icing agents
XF3	High water saturation, without de-icing agents	Horizontal concrete surfaces exposed to rain and freezing
XF4	High water saturation with de-icing agents or sea water	Road and bridge decks exposed to de-icing agents Concrete surfaces exposed to direct spray containing de-icing agents and freezing Splash zone of marine structures exposed to freezing
<b>6. Chemical attack</b>		
XA1	Slightly aggressive chemical environment according to EN 206-1, Table 2	Natural soils and ground water
XA2	Moderately aggressive chemical environment according to EN 206-1, Table 2	Natural soils and ground water
XA3	Highly aggressive chemical environment according to EN 206-1, Table 2	Natural soils and ground water

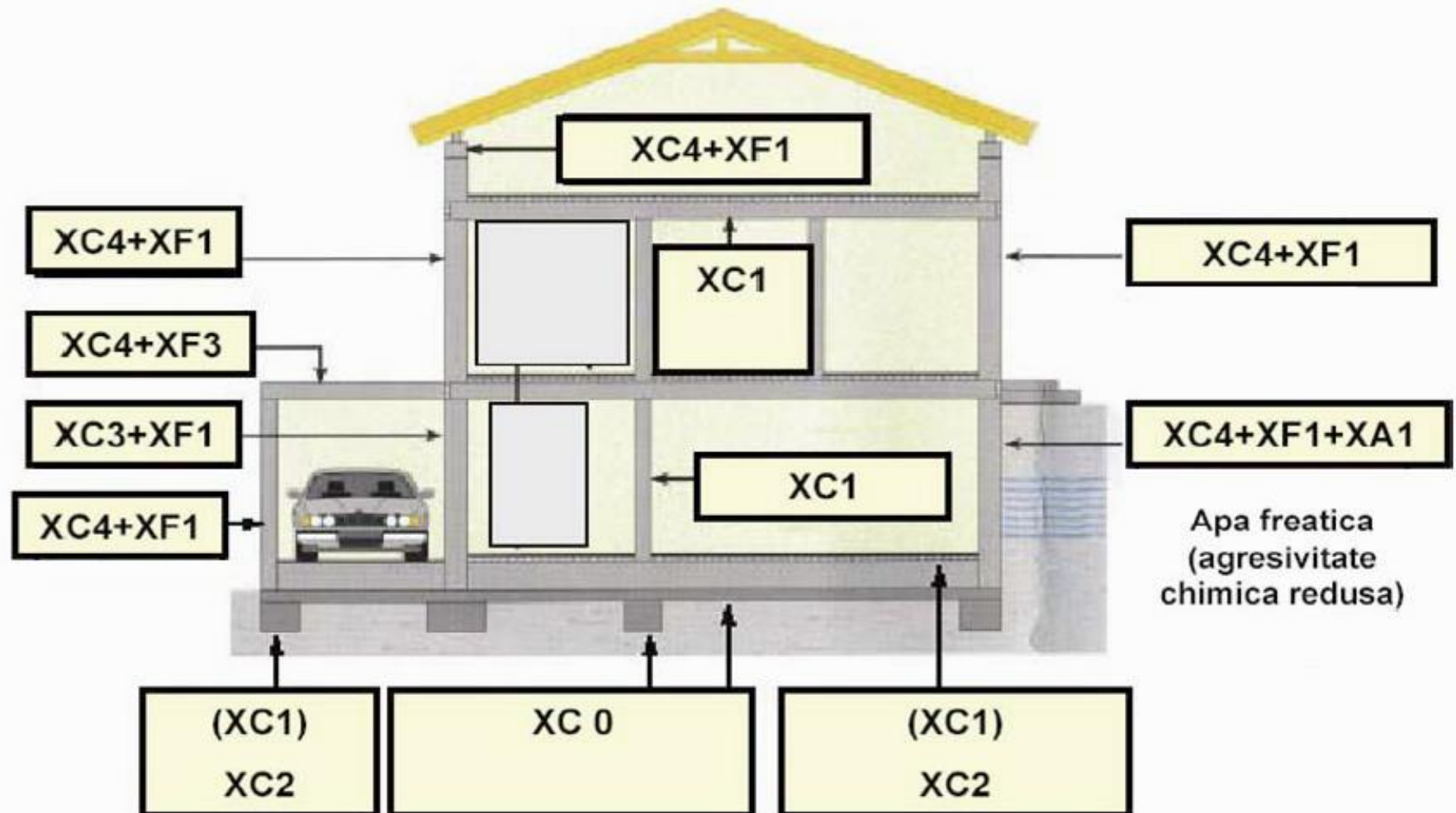
## Durability / Durabilitatea

## Reinforcement corrosion - superposed effects



## Durability / Durabilitatea

## Reinforcement corrosion - superposed effects



## Durability / Durabilitatea

### Strategies considered for increasing sustainability:

#### A. **Avoidance of degradation reactions** - is obtained by:

- "environmental change" application of membrane elements, protective films, etc.;
- chose of non-reactive materials: stainless steel, coated reinforcement, non-reactive aggregates, sulfates resistant cements ;
- reactions inhibition by cathodic protection, use of air entraining admixtures to to increase freeze-thaw resistance.

#### B. **The selection of the optimum materials and compositions**, suitable to resist to the expected degradation reactions

- suitable concrete composition;
- concrete cover thickness related to the environmental conditions;
- applying appropriate technologies for compacting concrete;
- increase the cross section of the elements resulted from the calculation, if is necessary

## Concrete cover

→ is the distance between the surface of the reinforcement closest to the nearest concrete surface (including links and stirrups and surface reinforcement where relevant) and the nearest concrete surface.

The concrete cover ensures:

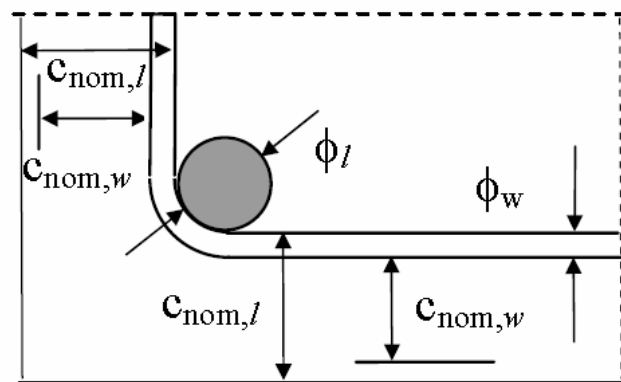
- Force transfer by bond from reinforcement to concrete
- Protection of steel rebars against corrosion (durability)
- An adequate fire resistance (not treated here)

The nominal cover shall be specified on the drawings !!! :

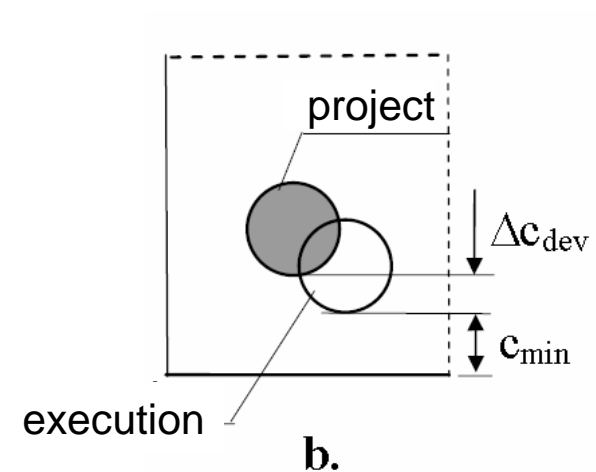
## Durability / Durabilitatea

$$c_{nom} = c_{min} + \Delta c_{dev}$$

$\Delta c_{dev}$  = 5 mm for cast-in-place slab (N. Annex)  
 = 10 mm for the rest of the element (A.N.)



**a.**  $c_{nom,l} \geq c_{nom,w} + \phi_w$



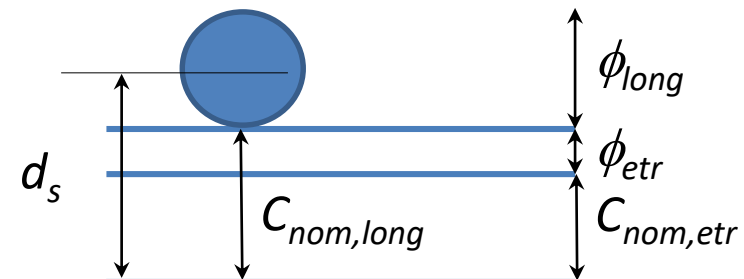
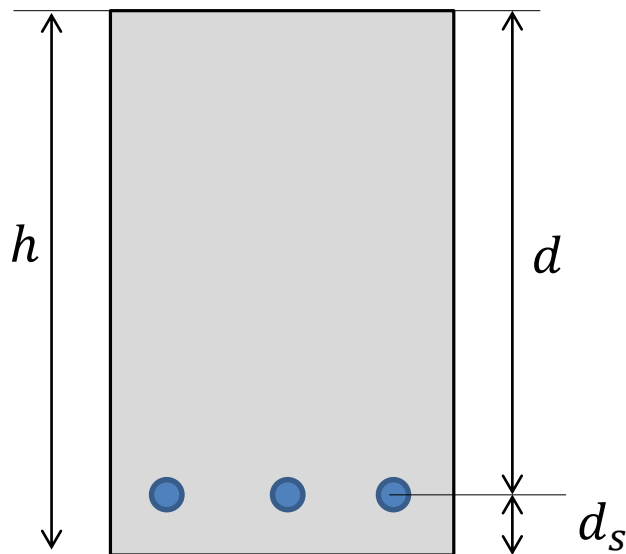
execution

**b.**



## Durability / Durabilitatea

$$c_{nom} = c_{min} + \Delta c_{dev}$$



## Durability / Durabilitatea

## Minimum concrete cover

$$c_{min} = \max \{c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm}\}$$

$$c_{min} = \max \left\{ \underbrace{c_{min,b}}_{\text{bond}}; \underbrace{c_{min,dur}}_{\text{durability}}; 10 \text{ mm} \right\}$$

- $c_{min,b}$  - minimum cover due to bond requirement
- $c_{min,dur}$  - minimum cover due to environmental conditions (N. Annex)
- $\Delta c_{dur,\gamma}$  - additive safety element (generally =0) (N. Annex)
- $\Delta c_{dur,st}$  - reduction of minimum cover for use of stainless steel (N. Annex)
- $\Delta c_{dur,add}$  - reduction of minimum cover for use of additional protection (N. Annex)

## Durability / Durabilitatea

## Minimum concrete cover

$$c_{min} = \max \left\{ \underbrace{c_{min,b}}_{\text{bond}}; \underbrace{c_{min,dur}}_{\text{durability}}; 10 \text{ mm} \right\}$$

$$c_{min,b} \geq \phi$$

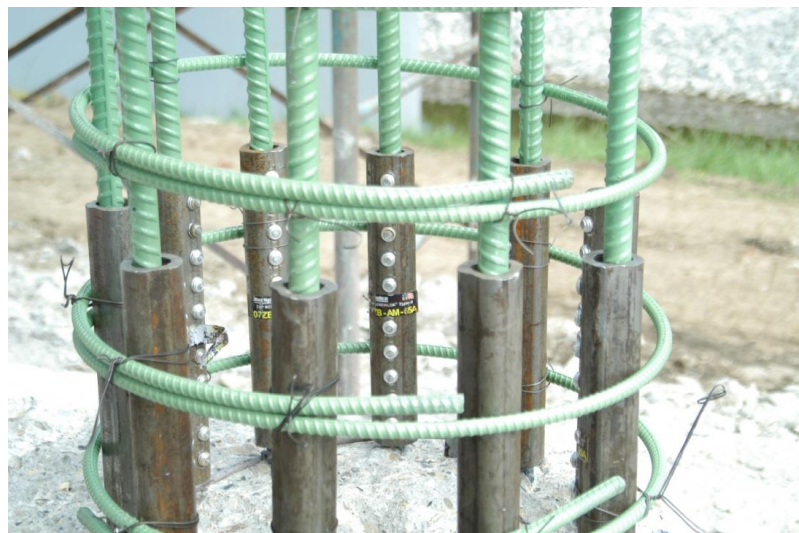
$c_{min,dur}$  = function of structural class (recommended S4 for a design working life of 50 years) and exposure class

Environmental Requirement for $c_{min,dur}$ (mm)							
Structural Class	Exposure Class according to Table 4.1						
	X0	XC1	XC2 / XC3	XC4	XD1 / XS1	XD2 / XS2	XD3 / XS3
S1	10	10	10	15	20	25	30
S2	10	10	15	20	25	30	35
S3	10	10	20	25	30	35	40
S4	10	15	25	30	35	40	45
S5	15	20	30	35	40	45	50
S6	20	25	35	40	45	50	55

## Durability / Durabilitatea

## Recommended structural classification

Structural Class							
Criterion	Exposure Class according to Table 4.1						
	X0	XC1	XC2 / XC3	XC4	XD1	XD2 / XS1	XD3 / XS2 / XS3
Design Working Life of 100 years	increase class by 2	increase class by 2	increase class by 2	increase class by 2	increase class by 2	increase class by 2	increase class by 2
Strength Class <sup>1)2)</sup>	≥ C30/37 reduce class by 1	≥ C30/37 reduce class by 1	≥ C35/45 reduce class by 1	≥ C40/50 reduce class by 1	≥ C40/50 reduce class by 1	≥ C40/50 reduce class by 1	≥ C45/55 reduce class by 1
Member with slab geometry (position of reinforcement not affected by construction process)	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1
Special Quality Control of the concrete production ensured	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1	reduce class by 1



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